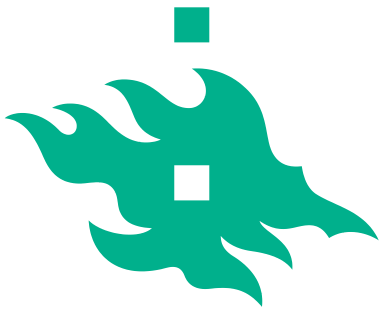


Animal breeding

Prof. Pekka Uimari

University of Helsinki

Department of Agricultural Sciences



Finnish dairy breeds



Ayrshire, Ay (66%)

Holstein, Hol (33%)



Production:
9400 kg, 3.9%, 3.3%

An average cow
produces 30 l milk per
day and 1 kg and
butter

Finncattle, Sk (1%)



Production:
6200 kg, 4.3%, 3.4%

Production: 8600 kg, 4.2%
fat, 3.4% protein

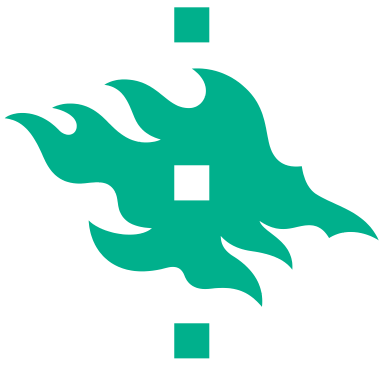
Average milk
production in Finland

1930: 2000 kg

1970: 4000 kg

1990: 5600 kg

2010: 8700 kg

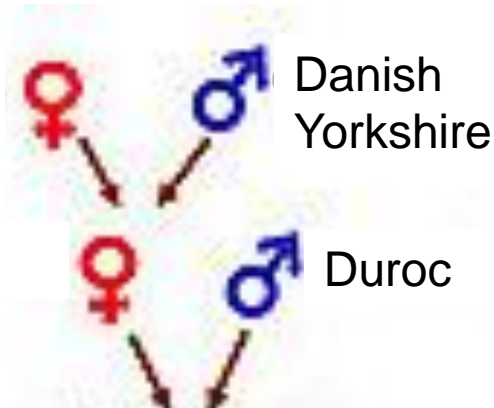


Two breeding programs for pigs in Finland

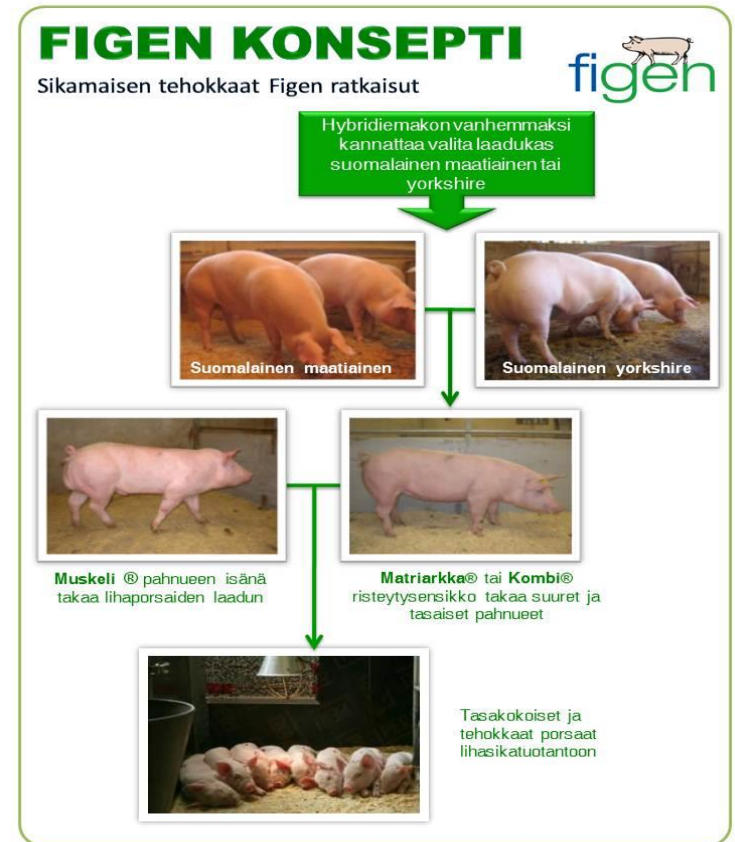


Norwegian
or Danish
Landrace

F1 sow



3 way cross
= pork





Tuotannon tarkkailu
Tilastolliset menetelmät
Genomitason tieto

Talous
Biologia
Ekologia
Etiikka

Jalostus-
arvostelu

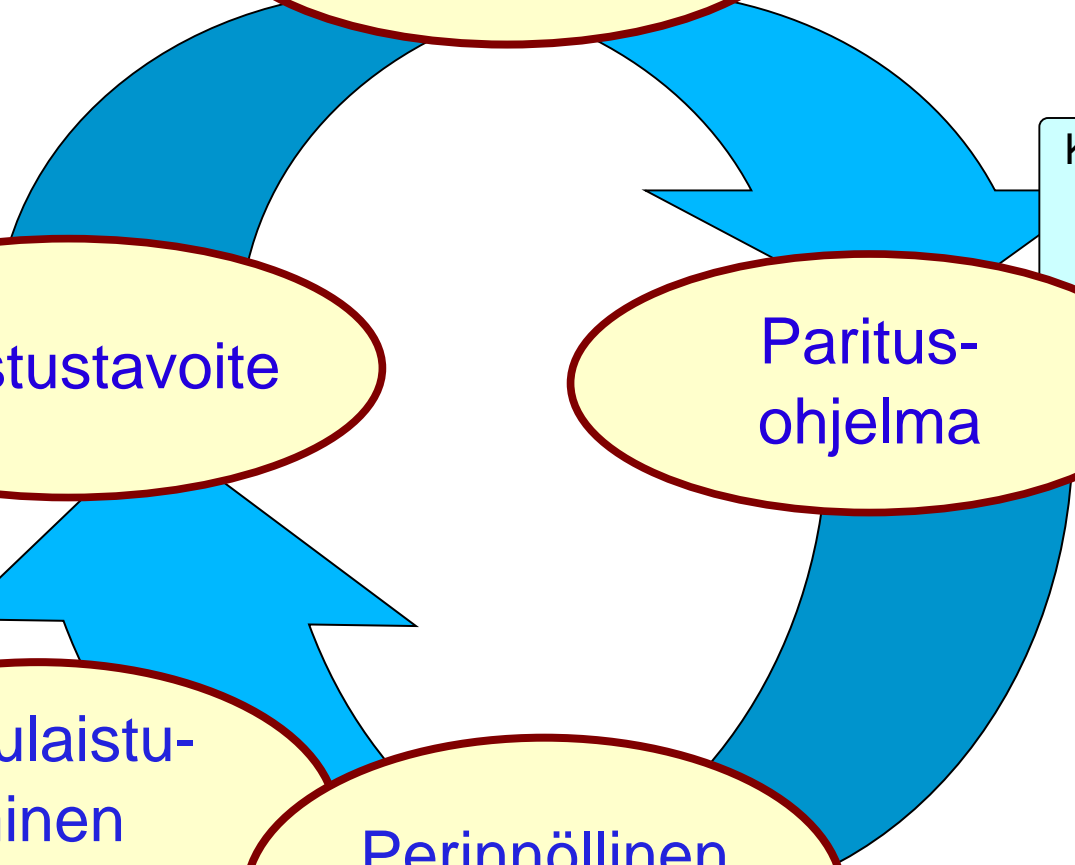
Keinosiemennys
Alkionsiirto

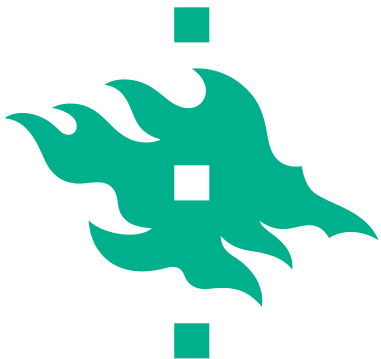
Jalostustavoite

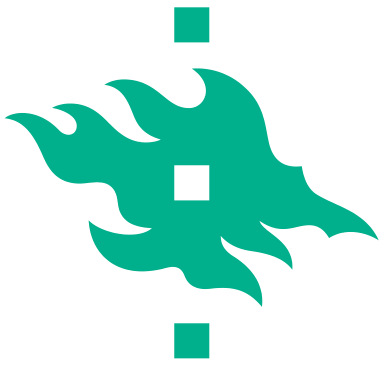
Paritus-
ohjelma

Sukulaistu-
minen
(sukusiitos)

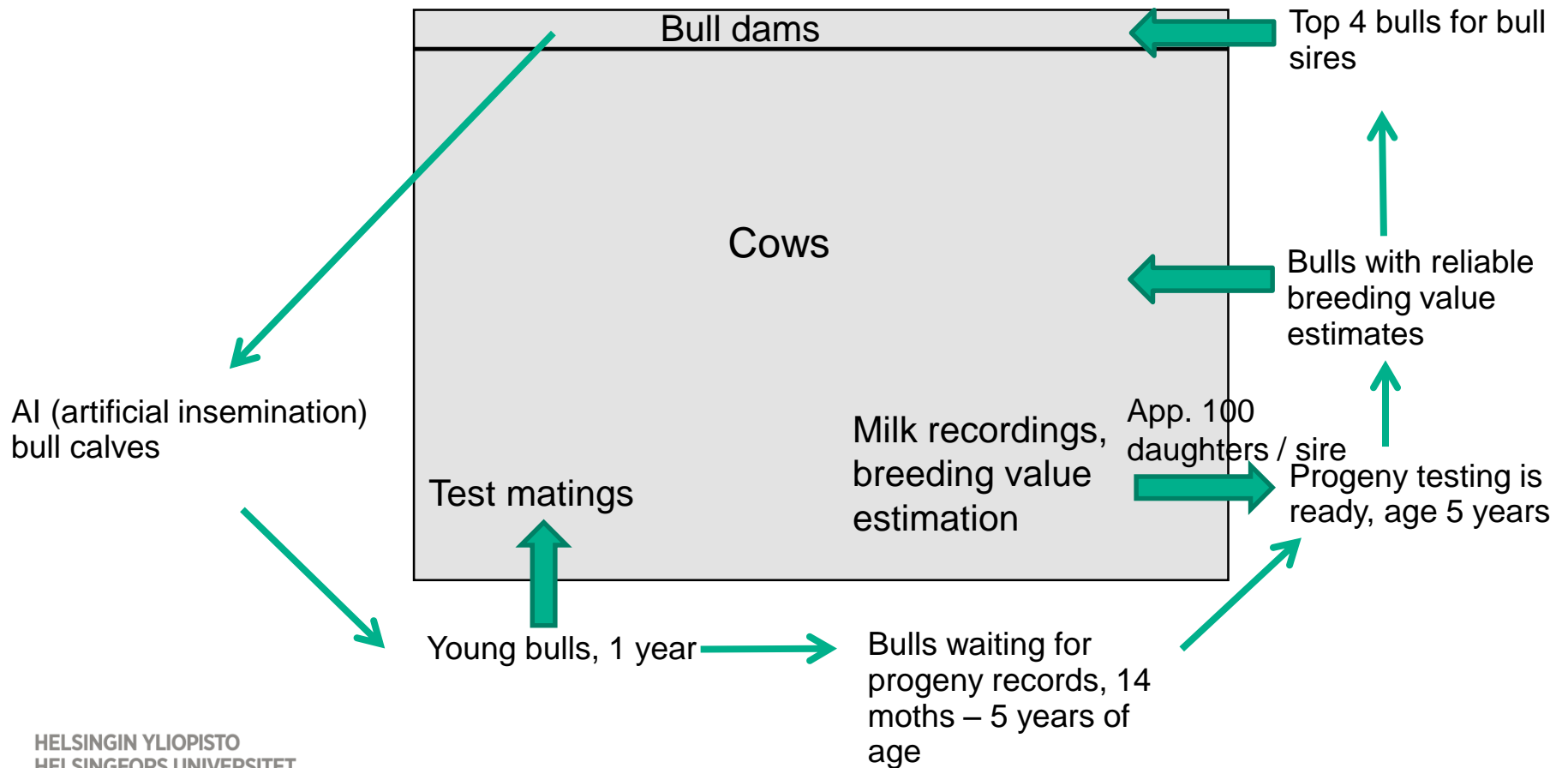
Perinnöllinen
edistyminen

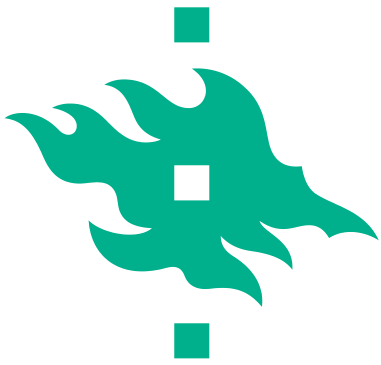






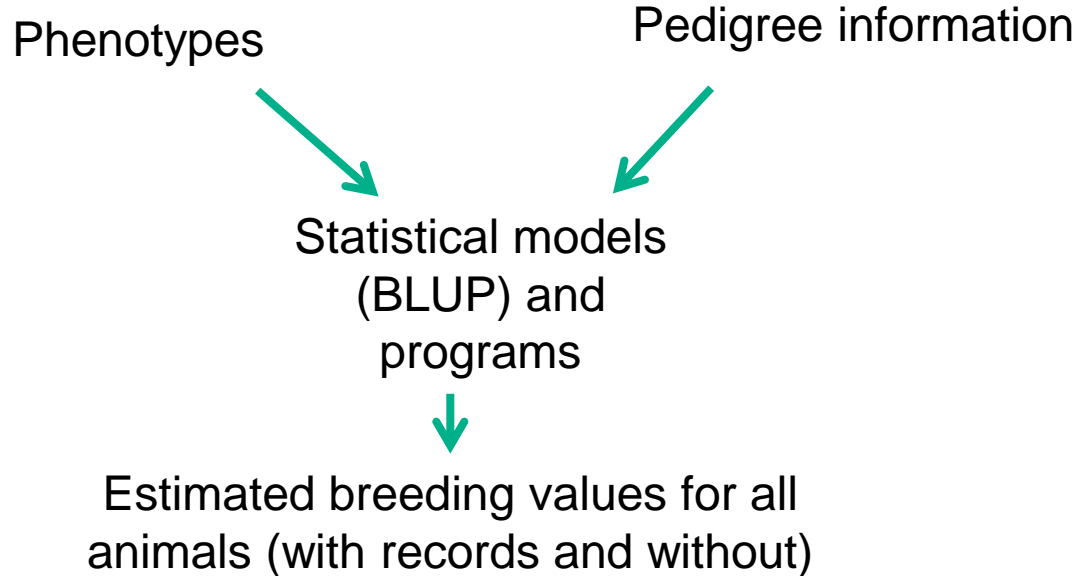
Traditional breeding program for dairy cows

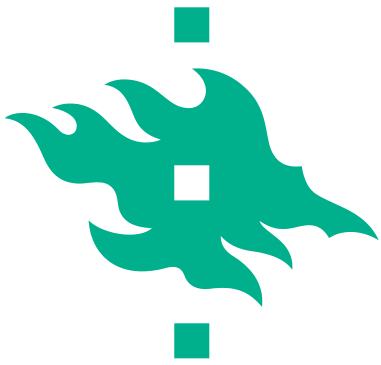




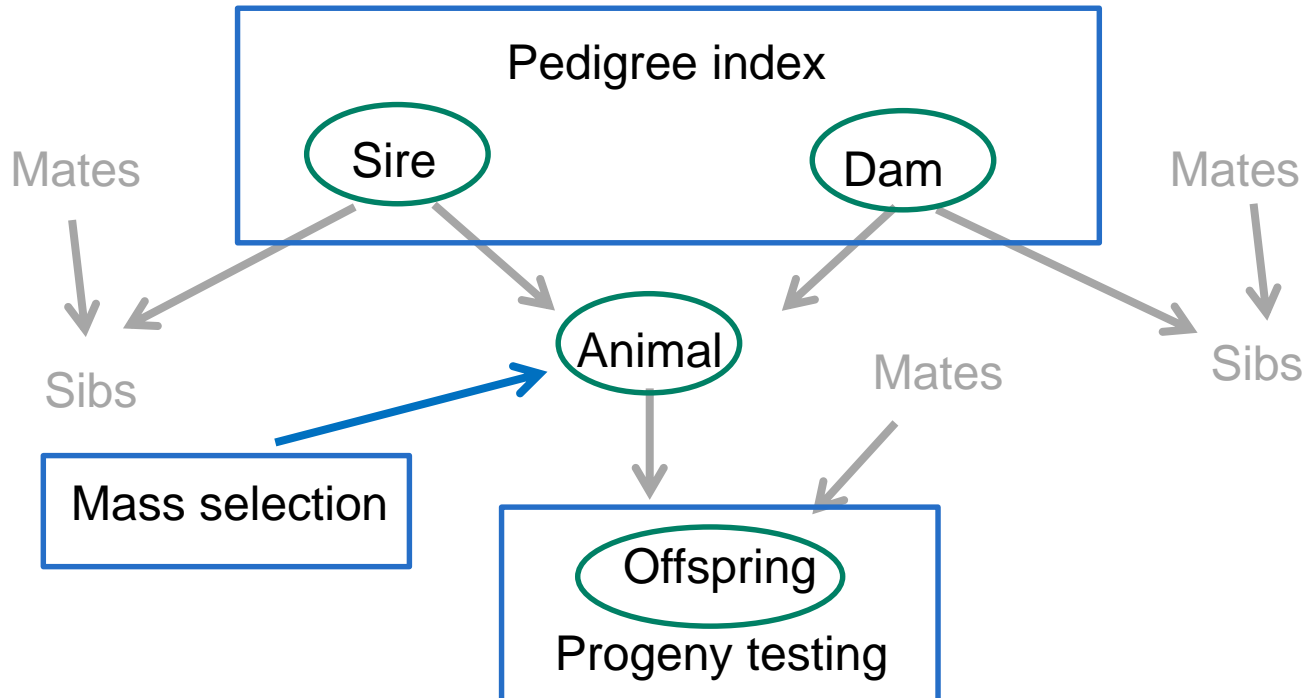
Traditional breeding value estimation

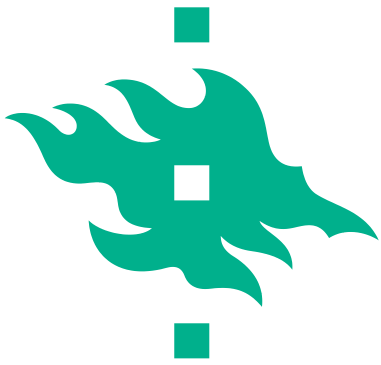
- Recorded measurements (phenotypes) such as milk production (dairy cows), litter size (pigs), health records etc.





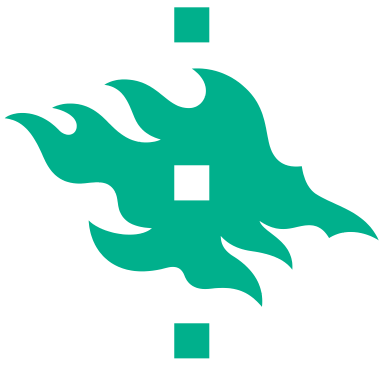
Information sources





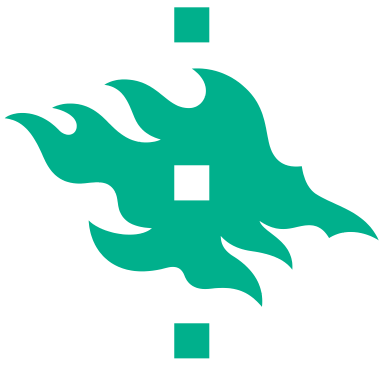
Traditional breeding value estimation

- Requires a large number of records
- Accuracy depends on heritability of the trait h^2
- Repeated measurements increase accuracy
- The number of offspring is important especially for traits that are sex specific such as milk production and litter size



Traditional breeding value estimation, steps

- Collection of phenotypic values
- Registry of pedigree → relationship between animals
- Linear mixed model:
 - Systematic environmental effects
 - Sex, age, herd, season, parity
 - Random effects
 - Permanent environment
 - Litter
 - Maternal effect
 - Animal itself (polygenic effect of the animal) ← relationship/kinship matrix
- Best linear unbiased prediction (BLUP) → Estimated breeding values EBV
- Standardization of the EBVs → Indices
- Publication of the results



Estimation of heritability

- Proportion of the phenotypic variation that is explained by genetic effects

$$h^2 = V_A / V_P$$

- Offspring on parent regression
 - $h^2 = 2 * b_{OP}$
- Twin data, correlation coefficient
 - $h^2 = 2(r_{MZ} - r_{DZ})$
 - MZ: monozygotic ("identical")
 - DZ: dizygotic

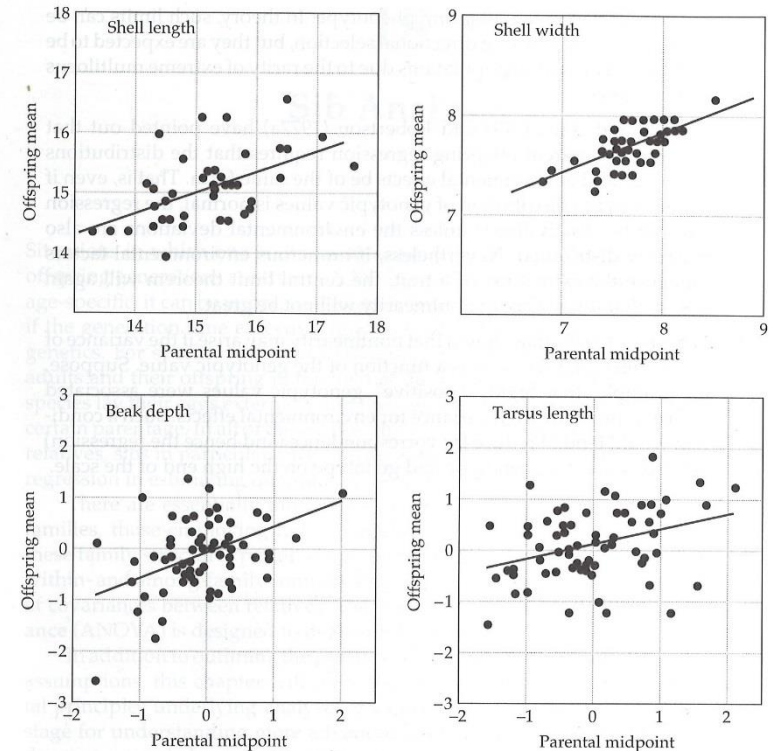
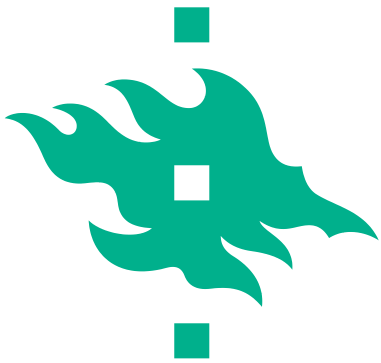


Figure 17.4 Examples of midparent-offspring regressions. Top panels: Land snail *Partula taeniata* (Murray and Clarke 1968). Bottom panels: Song sparrow *Melospiza melodia* (Smith and Zach 1979).



Estimation of heritability

SIB ANALYSIS 555

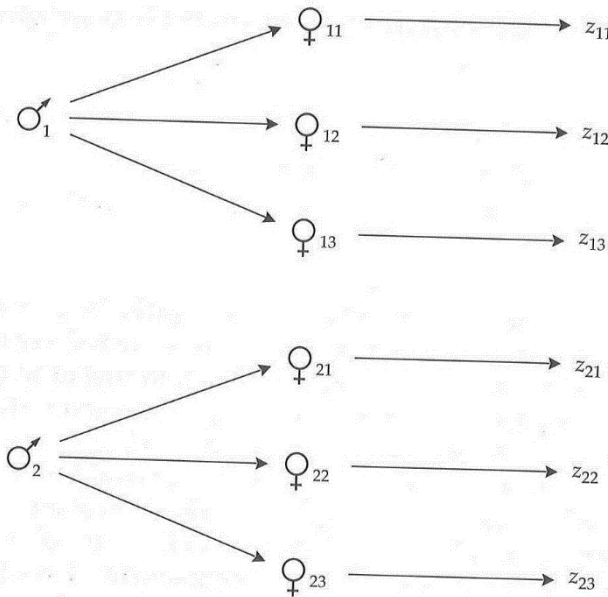
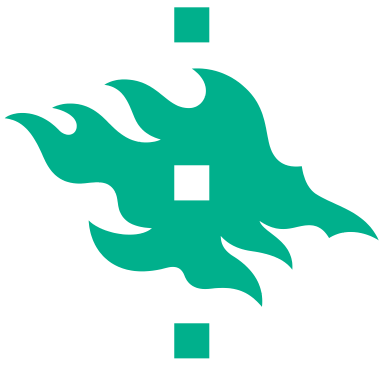


Figure 18.1 A paternal half-sib mating design. Each male is mated to several unique (unrelated) females, and a single offspring from each female is assayed.



Estimation of heritability

SIB ANALYSIS 559

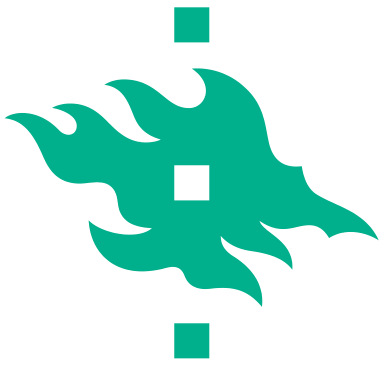
Table 18.1 Summary of a one-way ANOVA involving N independent families, the i th of which contains n_i individuals.

Factor	df	SS	MS	$E(\text{MS})$
Among-families	$N - 1$	$SS_s = \sum_{i=1}^N n_i (\bar{z}_i - \bar{z})^2$	$SS_s / (N - 1)$	$\sigma_e^2 + n_0 \sigma_s^2$
Within-families	$T - N$	$SS_e = \sum_{i=1}^N \sum_{j=1}^{n_i} (z_{ij} - \bar{z}_i)^2$	$SS_e / (T - N)$	σ_e^2
Total	$T - 1$	$SS_T = \sum_{i=1}^N \sum_{j=1}^{n_i} (z_{ij} - \bar{z})^2$	$SS_T / (T - 1)$	σ_z^2

Note: The total sample size is $T = \sum_{i=1}^N n_i$, and $n_0 = [T - (\sum n_i^2 / T)] / (N - 1)$, which reduces to n with equal family sizes. Degrees of freedom are denoted by df, observed sums of squares by SS, and expected mean squares by $E(\text{MS})$.

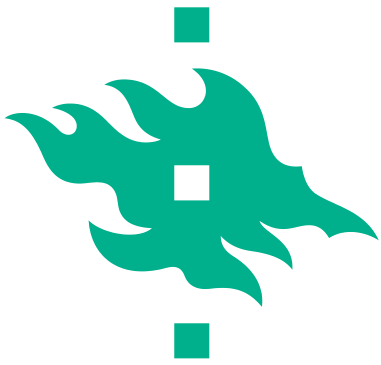
$$t_{\text{PHS}} = \frac{\text{Var}(s)}{\text{Var}(z)}$$

$$h^2 \simeq 4t_{\text{PHS}}$$



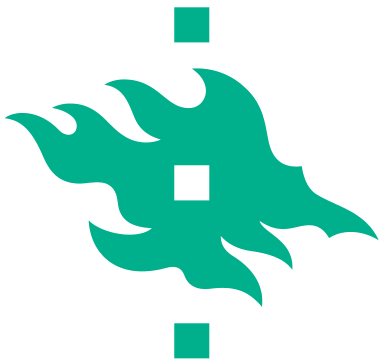
Estimation of heritability

- Usually we do not have balanced design
- Also fixed effects need to be counted
- For more general designs or pedigrees ANOVA-type of methods cannot be used
- REML (restricted maximum likelihood method)
 - Under strong development in 80's and 90's
 - Computational aspects needs lot of attention
 - Iterative solutions: average information and/or EM algorithm



Estimation of breeding values

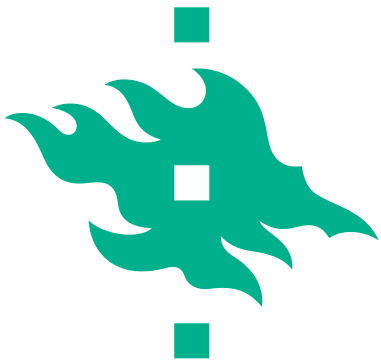
- Information sources
 - Pedigree information → relationship matrix A
 - Phenotypic records (y -values)
 - Systematic effects (gender, year) Fixed effects
 - Random effects (animal, permanent environment etc)
 - Variance components related to random effect → h^2
- Form a mixed linear model
- Form mix model equations
- Solve the equations
 - Iterative methods → no need to invert large matrices



Estimation of breeding values

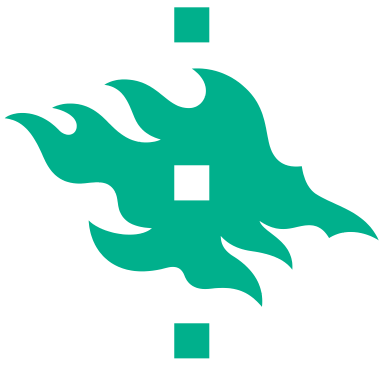
Matrix notation for BLUP

$$\begin{bmatrix} X'X & X'Z \\ Z'X & Z'Z + A^{-1} \sigma_e^2 / \sigma_a^2 \end{bmatrix} \begin{bmatrix} b \\ \hat{a} \end{bmatrix} = \begin{bmatrix} X'y \\ Z'y \end{bmatrix}$$



Estimation of breeding values

$$\begin{bmatrix} \mathbf{b} \\ \hat{\mathbf{a}} \end{bmatrix} = \begin{bmatrix} \mathbf{X}'\mathbf{X} & \mathbf{X}'\mathbf{Z} \\ \mathbf{Z}'\mathbf{X} & \mathbf{Z}'\mathbf{Z} + \mathbf{A}^{-1} \sigma_e^2 / \sigma_a^2 \end{bmatrix}^{-1} \begin{bmatrix} \mathbf{X}'\mathbf{y} \\ \mathbf{Z}'\mathbf{y} \end{bmatrix}$$



Estimation of breeding values

- The linear model needs to take into account all sources of factors that can have an effect on the phenotype
- Here is an example of the direct genetic, maternal and permanent environmental effects, all are treated as random effects

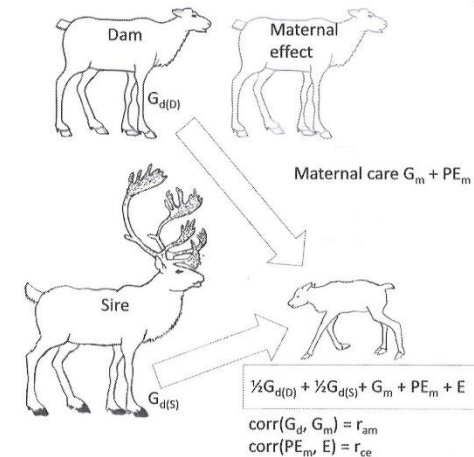
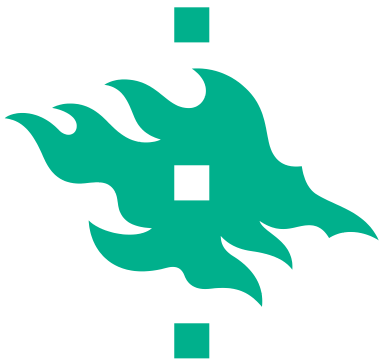


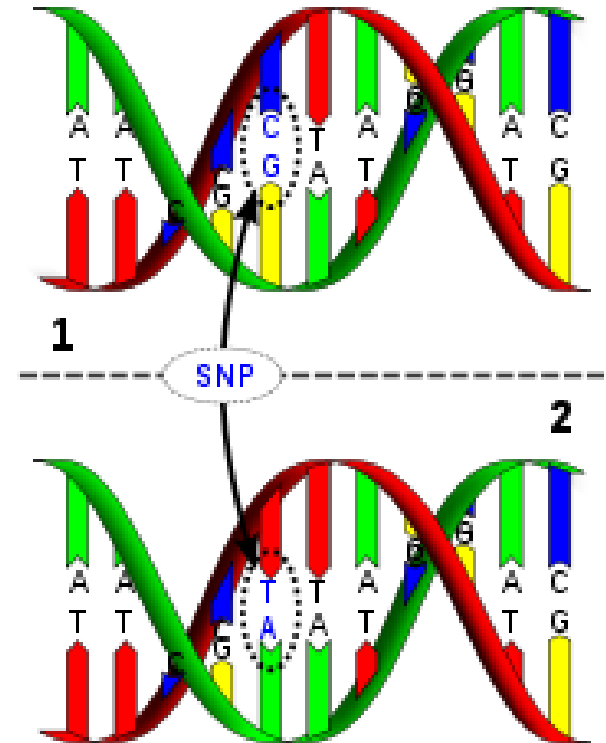
Figure 1 Direct and maternal effects on offspring phenotype. The direct effect (G_d) is split into the sire's (S) and dam's (D) additive genetic effect. The maternal effect consists of the maternal genetic effect (G_m), maternal permanent environmental effect (PE_m) and maternal temporary environmental effect (E_m). The direct-maternal genetic correlation is denoted as r_{dm} and the respective direct-maternal environmental correlation as r_{ce} (the reindeer figures are modifications of those by Mauri Nieminen).

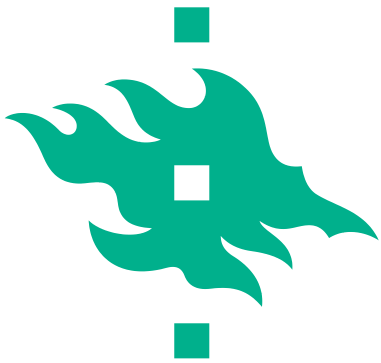
Kirsi Muuttoranta, PhD thesis



SNP: single nucleotide polymorphism

- DNA sequence variations that occur when a single nucleotide (A, T, C, or G) in the genome sequence is altered

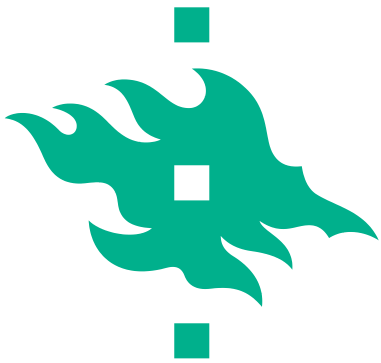




Commercial chips

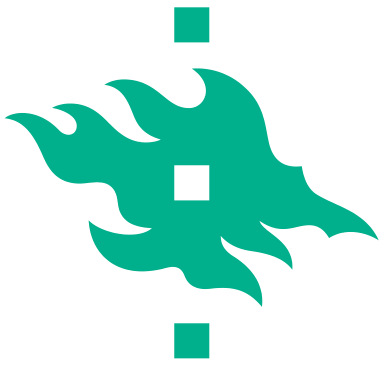
- Illumina:
 - BovineLD
 - BovineSNP50
 - BovineHD
 - PorcineSNP60
 - OvineSNP50
- Affymetrix
 - Axiom Genome-Wide BOS 1 Array
- Price 20-100€/sample





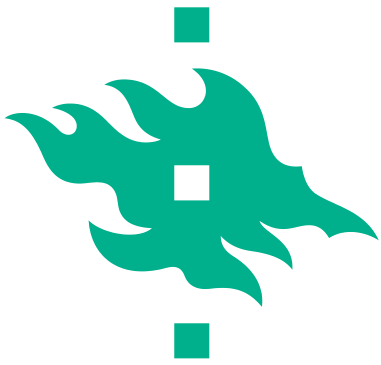
Applications of the SNP chips

- Genomic selection
 - Applied mainly in dairy cattle breeding
- Gene mapping
 - Single gene Mendelian traits
 - Polygenic traits
 - More powerful than microsattellites because the high density of SNPs allow linkage disequilibrium based gene mapping methods
→ the causal mutation can be mapped with more precise position

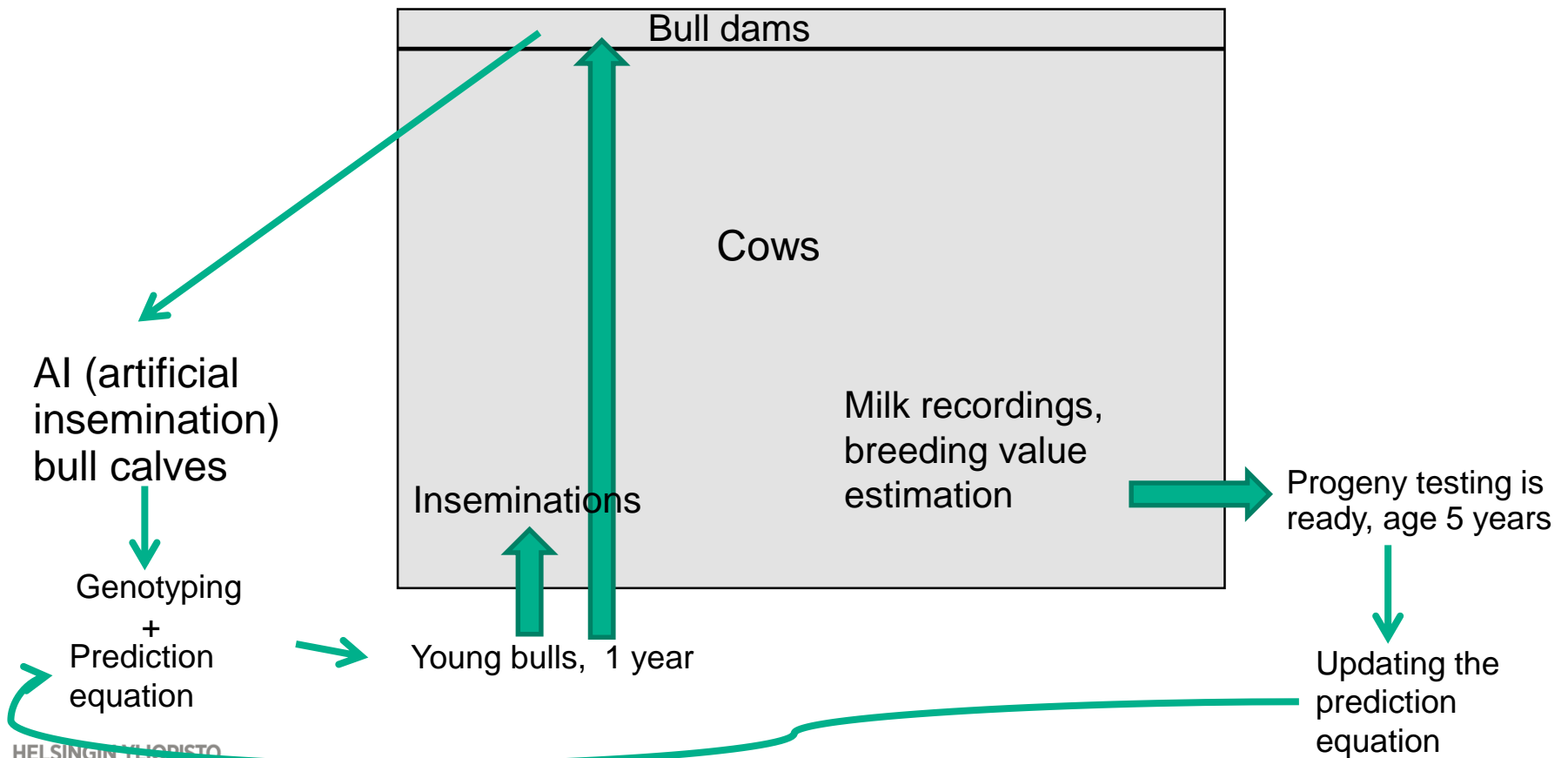


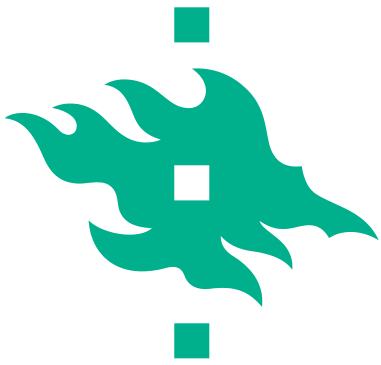
Genomic selection

- Genomic selection is the biggest biotechnological revolution in animal breeding since artificial insemination
- Moderate price of chips has enabled genotyping of thousands (millions) of production animals
- New statistical methods and programs have been developed to combine genotypic and phenotypic information in breeding value evaluation
- Genetic merit == breeding value of a animal can be predicted from it's DNA → generation interval is short → important especially in dairy and beef cattle



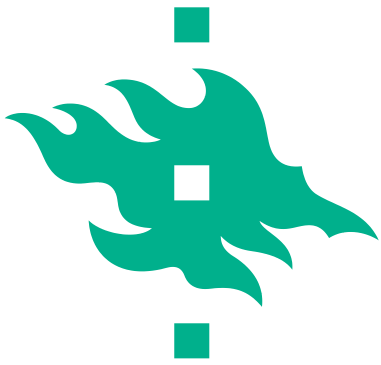
An example of genomic selection in dairy cattle





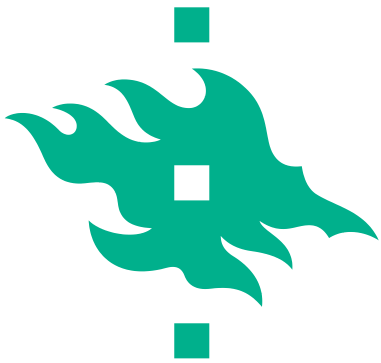
Prediction equation

- Reference population is needed
- Animals with reliable estimates of breeding values: AI-bulls (boars) with tens to hundreds of progeny
- These animals will be genotyped (sperm, blood, hair samples)
- The number of animals in reference population varies from hundreds to thousands, Eurogenomics >25,000 AI-bulls + tens of thousands of cows



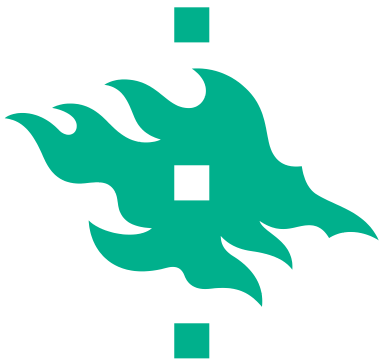
Prediction equation

- Statistical methods to estimate effect of each SNP on production
- A separate prediction model must be estimated for each trait and population
- SNPs that have the biggest effect on the trait will have the biggest weight in the equation
- Accuracy of breeding value estimates based on genomic selection varies from 50 to 80% depending on the size of the reference population, trait and homogeneity of the population



SNP-BLUP

- SNP-BLUP, mixed model:
- $\mathbf{y} = \mathbf{1}\mu + \mathbf{Z}\mathbf{g} + \mathbf{e}$;
 - \mathbf{y} is vector of observations (reference animals)
 - μ is the general mean,
 - \mathbf{Z} is a $n \times m$ matrix containing a column for each marker locus,
 - \mathbf{g} is a vector of length m of random SNP marker effects
 - \mathbf{e} random residual effect
- An assumption: $\mathbf{g} \sim N(0, \mathbf{I}\sigma^2_g)$



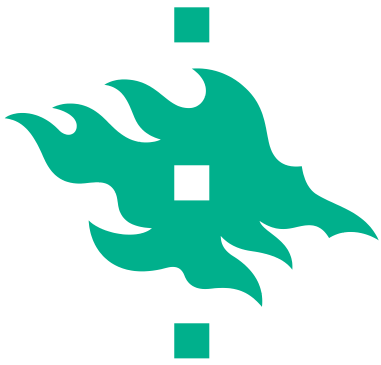
SNP-BLUP

Matrix notation for SNP-BLUP

$$\begin{bmatrix} \mathbf{1}'\mathbf{1} & \mathbf{1}'\mathbf{Z} \\ \mathbf{Z}'\mathbf{1} & \mathbf{Z}'\mathbf{Z} + \mathbf{I}\sigma_e^2/\sigma_g^2 \end{bmatrix} \begin{bmatrix} \mu \\ \hat{\mathbf{g}} \end{bmatrix} = \begin{bmatrix} \mathbf{1}'\mathbf{y} \\ \mathbf{Z}'\mathbf{y} \end{bmatrix}$$

Scalar notation for 5 SNPs:

$$y_i = \mu + z_i g_1 + z_i g_2 + z_i g_3 + z_i g_4 + z_i g_5 + e_i$$



Genomic breeding values (GEBV) or direct genomic values (DGV)

$$\text{GEBV} = \mu + \mathbf{Z}\hat{\mathbf{g}}$$

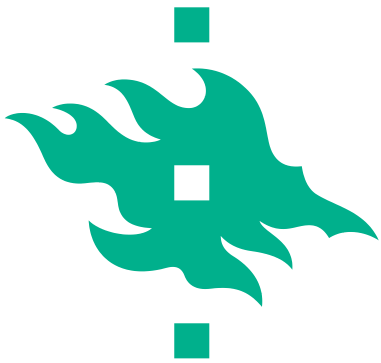
For 5 SNPs and animal i:

$$\text{GEBV}_i = \mu + z_i\hat{g}_1 + z_i\hat{g}_2 + z_i\hat{g}_3 + z_i\hat{g}_4 + z_i\hat{g}_5$$

Hypothetical example:

$$\text{GEBV}_i = 2.3 + 1*0.02 + 0*0.01 + 2*0.02 + 2*(-0.01) + 0*0.01$$

$$\text{GEBV}_i = 2.34$$



GBLUP

Matrix notation for GBLUP

$$\begin{bmatrix} \mathbf{1}'\mathbf{1} & \mathbf{1}' \\ \mathbf{1} & \mathbf{I} + \lambda\mathbf{G}^{-1} \end{bmatrix} \begin{bmatrix} \boldsymbol{\mu} \\ \hat{\mathbf{a}} \end{bmatrix} = \begin{bmatrix} \mathbf{1}'\mathbf{y} \\ \mathbf{Z}'\mathbf{y} \end{bmatrix}$$

\mathbf{G}^{-1} is the genomic relationship matrix

$\lambda = \sigma_e^2 / \sigma_g^2$ and $\text{GEBV} = \boldsymbol{\mu} + \hat{\mathbf{a}}$