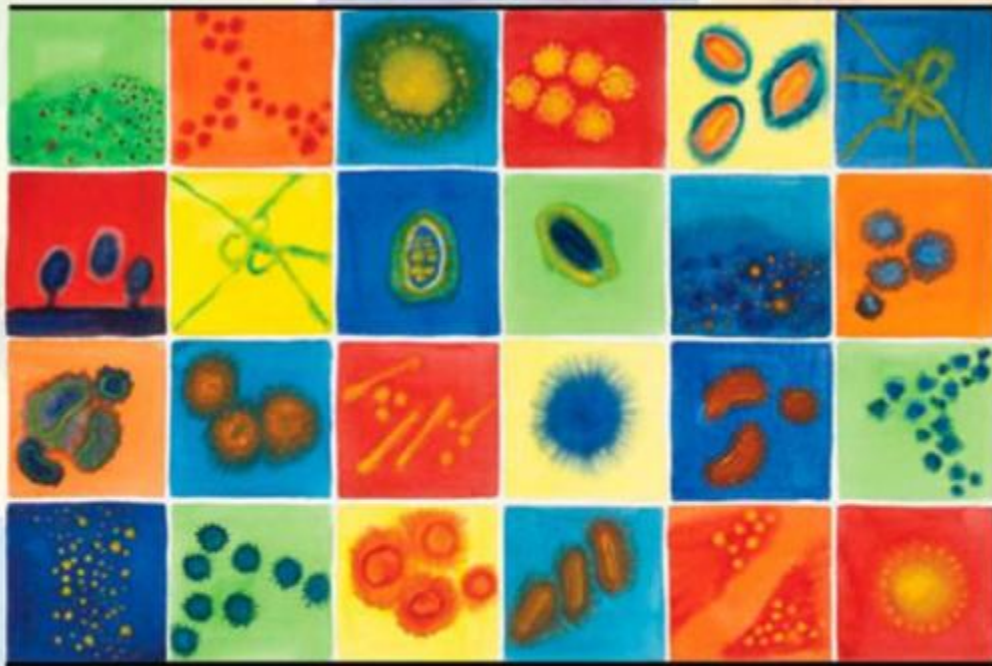


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Mathematical Tools for Understanding Infectious Disease Dynamics

PRINCETON SERIES IN THEORETICAL AND COMPUTATIONAL BIOLOGY



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