

```

dx[x_, y_] := f[x] - g[x] y;
dy[x_, y_] :=  $\gamma$  g[x] y -  $\delta$  y -  $\epsilon$  y2;

f[x_] := x (1 - x);
g[x_] :=  $\beta$  x (1 +  $\beta$  T x)-1;

 $\beta = 5$ ;  $\gamma = 1$ ;  $\delta = .1$ ;  $\epsilon = 1$ ; T = 1;

{x, y} /. Solve[{dx[x, y] == 0, dy[x, y] == 0}, {x, y}] // N

{{0., -0.1}, {0., 0.}, {1., -5.32907  $\times 10^{-16}$ }, {0.124821, 0.284277},
{0.237589 - 0.651336 i, 0.757862 - 0.211568 i}, {0.237589 + 0.651336 i, 0.757862 + 0.211568 i}}

{xEq, yEq} = {0.1248211895843873`, 0.2842766222982483`}

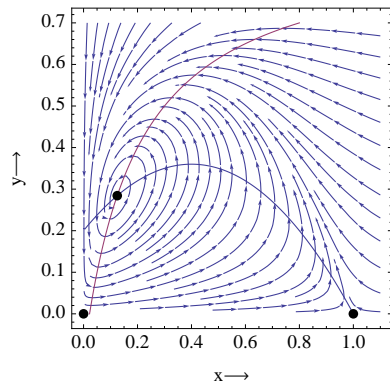
{0.124821, 0.284277}

```

```

Show[
{
StreamPlot[{dx[x, y], dy[x, y]}, {x, 0, 1.1}, {y, 0, .7}],
ContourPlot[{dx[x, y], dy[x, y]}, {x, 0, 1.1}, {y, 0, .7}, PlotPoints -> 100],
Graphics[{PointSize[Medium], Point[{0, 0}, {1, 0}, {xEq, yEq}]}]}],
FrameLabel -> {"x->", "y->"}, ImageSize -> Small]

```



```

A = {{a11, a12}, {a21, a22}} = D[{dx[x, y], dy[x, y]}, {{x, y}}] /. {x -> xEq, y -> yEq};

```

```

MatrixForm[A]

```

```

( 0.21149  -0.384277 )
( 0.538868 -0.284277 )

```

```

Det[A]

```

```

0.146953

```

```

Tr[A]

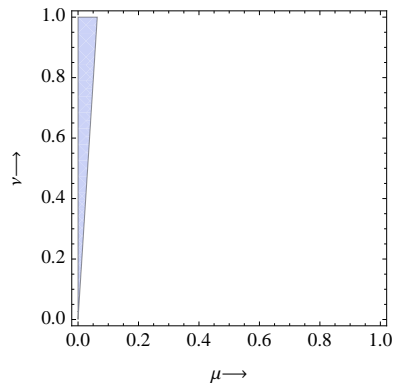
```

```

-0.0727871

```

```
RegionPlot[ $\mu a_{22} + \nu a_{11} > 2 \sqrt{\mu \nu \text{Det}[A]}$ , { $\mu$ , 0, 1},
{ $\nu$ , 0, 1}, FrameLabel -> {" $\mu \rightarrow$ ", " $\nu \rightarrow$ "}, ImageSize -> Small]
```



```
Id = {{1, 0}, {0, 1}};
Di = {{ $\mu$ , 0}, {0,  $\nu$ }};
```

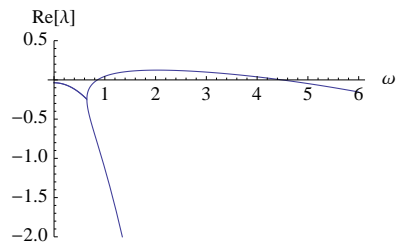
```
CharEq = Det[ $\lambda$  Id - A +  $\omega^2$  Di] == 0
```

```
0.146953 + 0.0727871  $\lambda$  +  $\lambda^2$  + 0.284277  $\mu \omega^2$  +  $\lambda \mu \omega^2$  - 0.21149  $\nu \omega^2$  +  $\lambda \nu \omega^2$  +  $\mu \nu \omega^4$  == 0
```

```
{ $\lambda_1$ ,  $\lambda_2$ } =  $\lambda$  /. Solve[CharEq,  $\lambda$ ] // Simplify
```

```
{-0.0363935 - 0.5  $\mu \omega^2$  - 0.5  $\nu \omega^2$  -
0.5  $\sqrt{(-0.582513 - 0.991532 \mu \omega^2 + 0.991532 \nu \omega^2 + 1. \mu^2 \omega^4 - 2. \mu \nu \omega^4 + 1. \nu^2 \omega^4)}$ , -0.0363935 -
0.5  $\mu \omega^2$  - 0.5  $\nu \omega^2$  + 0.5  $\sqrt{(-0.582513 - 0.991532 \mu \omega^2 + 0.991532 \nu \omega^2 + 1. \mu^2 \omega^4 - 2. \mu \nu \omega^4 + 1. \nu^2 \omega^4)}$ }
```

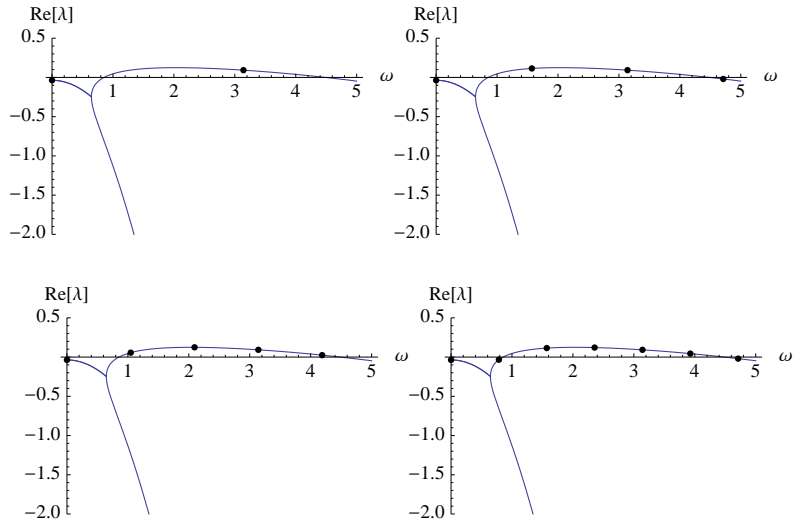
```
Plot[Re[{ $\lambda_1$ ,  $\lambda_2$ } /. { $\mu \rightarrow .01$ ,  $\nu \rightarrow 1$ }], { $\omega$ , 0, 6},
PlotRange -> {-2, .5}, AxesLabel -> {" $\omega$ ", "Re[ $\lambda$ "]}, ImageSize -> Small]
```



```

μ = .01; ν = 1; ωMax = 6;
Row[
  Table[
    Show[
      Plot[Re[{λ1, λ2}], {ω, 0, 5}, PlotRange → {-2, .5}],
      Graphics[
        Point[Table[{k π / L, Max[Re[{λ1, λ2}] /. {ω → k π / L}]}], {k, 0, ωMax L / π, 1}]]],
      AxesLabel → {"ω", "Re[λ]"}, ImageSize → Small],
    {L, 1, 4}]
]

```



L = 3;

```

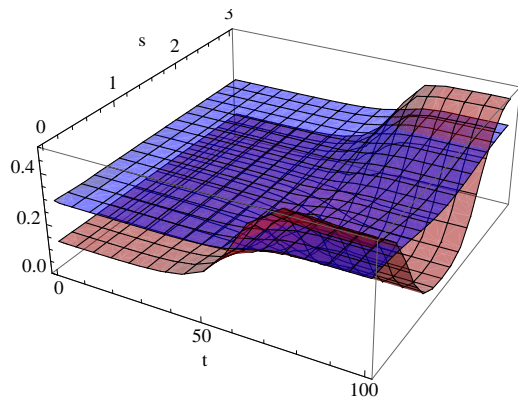
equations = {
  x(1,0)[t, s] == f[x[t, s]] - g[x[t, s]] y[t, s] + μ x(0,2)[t, s],
  y(1,0)[t, s] == γ g[x[t, s]] y[t, s] - δ y[t, s] - ε y[t, s]2 + ν y(0,2)[t, s],
  x(0,1)[t, 0] == 0,
  x(0,1)[t, L] == 0,
  y(0,1)[t, 0] == 0,
  y(0,1)[t, L] == 0,
  x[0, s] == xEq (1 + .01 (Random[] - .5) ∑k=110 Cos[ $\frac{k \pi s}{L}$ ]),
  y[0, s] == yEq (1 + .01 (Random[] - .5) ∑k=110 Cos[ $\frac{k \pi s}{L}$ ])
};

```

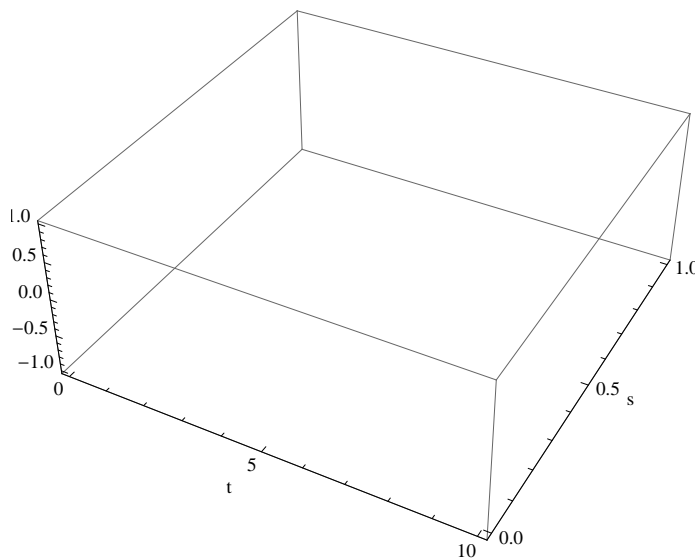
```
NDSolve[equations, {x, y}, {t, 0, 100}, {s, 0, L}]
```

```
Plot3D[Evaluate[{x[t, s], y[t, s]} /. %], {t, 0, 100}, {s, 0, L}, PlotRange -> {0, .5},
  PlotStyle -> {Directive[Opacity[0.7], Red], Directive[Opacity[0.7], Blue]},
  AxesLabel -> {"t", "s", ""}]
```

```
{x -> InterpolatingFunction[{{0., 100.}, {0., 3.}], <>],
 y -> InterpolatingFunction[{{0., 100.}, {0., 3.}], <>}}
```



```
Plot3D[Evaluate[{x[t, s], y[t, s]} /. %], {t, 0, 10}, {s, 0, 1},
  PlotStyle -> {Directive[Opacity[0.7], Red], Directive[Opacity[0.7], Blue]},
  AxesLabel -> {"t", "s", ""}]
```



```
yEq
```

```
0.284277
```