## Topic suggestions for project works in the course "Sobolev spaces"

1. Characterization of traces of  $W^{1,p}(\Omega)$ -functions by Besov spaces.

Taken/Varattu

- Interior regularity of solutions to elliptic PDE's. Taken/Varattu
- 3. Second-order hyperbolic equations.

Taken/Varattu

4. Fredholm's alternative, Dirichlet eigenvalues and the spectrum of the Laplacian in bounded smooth domains.

Taken/Varattu

5. Time dependent Sobolev spaces and the heat equation.

Taken/Varattu

6. Operator semigroups, Hille-Yosida theorem and hyperbolic equations.

Taken/Varattu

7. Differentiability of Sobolev functions, Rademacher's theorem and absolute continuity along a.e. line.

8. Maximal functions and Sobolev spaces.

Taken/Varattu

- Riesz-potentials and Poincare inequalities, including weighted spaces. Taken/Varattu
- Calculus of variations: non-linear elasticity and polyconvex functionals. Taken/Varattu

11. Calculus of variations: Harmonic mappings and constrained variational problems.

Taken/Varattu

- 12. Maximum principles and elliptic PDE's.
- 13. Hamilton Jacobi Equations.

Taken/Varattu

- 14. Fourier analysis methods in Sobolev spaces,  $H^{1/2}$  and the trace theorem. Taken/Varattu
- 15. Sobolev spaces and second order parabolic equations.
- 16. Nonlinear eigenvalue problems.

Taken/Varattu