

**Matematiikan ja tilastotieteen laitos**  
**Topics in geometric Fourier analysis**  
**Exercise 1**  
**2.2.2012**

1. Prove Riemann-Lebesgue lemma.
2. Prove formulas (1.10) and (1.11).
3. Prove the assertion (1.9).
4. What is the Fourier transform of the sign function  $sgn$ ;  $sgn(x) = 1$ , when  $x \geq 0$ ,  $sgn(x) = -1$ , when  $x < 0$ ?
5. Prove formulas (1.18)-(1.20).
6. Show that if  $\mu$  is a finite Borel measure on  $\{x, 0) \in \mathbb{R}^2 : x \in \mathbb{R}\}$ , then  $\hat{\mu}(\xi)$  does not tend to 0 as  $|\xi| \rightarrow \infty$ .