

1. Use a table of z-scores to determine the following proportions:
  - (a) below  $z = 1.5$
  - (b) below  $z = -0.085$
  - (c) above  $z = 2.8$
  - (d) above  $z = -1.09$
  - (e) between  $z = 1.5$  and  $z = 2.8$
  - (f) between  $z = -2.455$  and  $z = 1.765$ .
2. Use a table of z-scores to determine the following z-values:
  - (a) the value below which 0.25 of the distribution falls
  - (b) the value below which 0.85 of the distribution falls
  - (c) the value above which 0.725 of the distribution falls
  - (d) the value above which 0.05 of the distribution falls.
3. Let  $X$  be a discrete random variable, and let  $a$  be such that  $\mathbb{P}(X = a) > 0$ . Show that  $\mathbb{P}(X \leq a) = \mathbb{P}(X < a) + \mathbb{P}(X = a)$ . How the equality changes if we let  $X$  be a continuous random variable.
4. A researcher collects opinion poll data in a busy shopping centre on support for public flogging for misdemeanours, and vegetarianism. The data is shown as a cross-tabulation of frequencies, below.

	Support flogging	Oppose flogging
Vegetarian	35	15
Meat eater	15	35

Assuming that this is a representative sample of the Finnish population

- (a) What is the probability that a Finn vegetarian supports flogging?
  - (b) What is the likelihood that a randomly selected person will be a meat eater, and support flogging?
  - (c) Can you think of any way in which we could use probability calculations to decide whether the variables “vegetarianism support” and “flogging support” are independent?
5. In a study to examine helping behaviour we ask a confederate (a little old lady) to pretend to collapse in the main road. We count the number of people that walk by before assistance is rendered. We repeat the procedure 2000 times over a period of one year. The data are normally distributed with a mean of 20 and a standard deviation of 5.
  - (a) If we assume that this is the data for the population of cases of helping behaviour, what is the probability that at least 35 people will walk past a little old lady who collapses in the main road?
  - (b) What is the 25th percentile of “helping behaviour”?

6. A Regional Football Association (RFA), has been advised by a team of social psychology consultants that crowd disturbances at football matches are much more likely to occur on very hot and very cold days. Apparently, these extreme weather conditions frustrate people, and this frustration easily boils over into crowd disturbances. RFA decide that they will call off any scheduled football match if the temperature is more extreme than it is 98.5% of the time. If the daily temperature is normally distributed with a mean of 22 and a standard deviation of 9, at what temperatures will RFA call off soccer matches?
7. A shop receives a batch of 1000 cheap lamps. The odds that a lamp is defective are 0.1%. Let  $X$  be the number of defective lamps in the batch.
  - (a) What kind of distribution does  $X$  have? What is/are the value(s) of parameter(s) of this distribution?
  - (b) What is the probability that the batch contains no defective lamps? One defective lamp? More than two defective ones?
8. The long-term average for the number of rainy days in Cape Town during the month of April is known to be 9.3, with a standard deviation of 3.6. What is the probability that a visitor to Cape Town in the month of April will experience more than 15 days of rain?