

## ADAPTIVEDYNAMICS

### Exercise 10-11

#### Exercise 12

This is a continuation of exercise 11 where we practiced to numerically calculate isoclines for the evolution of a dimorphic population. We now practice to numerically calculate solutions of the canonical equation (CE) and orbits of the stochastic differential equation (SDE) as approximations of substitution sequences.

Consider the Lotka-Volterra competition model with  $K(x) = e^{-(x-\delta)^4} + e^{-(x+\delta)^2}$  and  $a(x, y) = e^{-\alpha(x-y)^2 - \beta(x-y)}$  with  $\alpha = 2.0$ ,  $\beta = -0.4$  and  $\delta = 1.0$ .

(a) Calculate numerically solutions of the canonical equation (CE) for a monomorphic resident population using the Euler integration method. Try different starting points.

(b) Calculate numerically solutions of the stochastic differential equation (SDE) in a monomorphic resident population using the Euler integration method. Try different starting points. For each starting point try different runs.

(c) Calculate numerically solutions of the canonical equation (CE) for a dimorphic resident population using the Euler integration method. As starting point, start inside the region of coexistence and near a branching point.

(d) Calculate numerically solutions of the stochastic differential equation (SDE) in a monomorphic resident population using the Euler integration method. As starting point, start inside the region of coexistence and near a branching point. Make several runs for the same starting point.

#### Exercise 13

In the same model as above, which of the singular points in the dimorphic resident population are *totally* stable, which are *strongly* stable and which are *weakly* stable. What do these different kinds of stability refer to?

N.B. after you have done the above exercises, feel free to vary the parameters.