

# From grass roots to galaxies: IP research at Tampere UT

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in Inverse Problems Research

# Research areas, plans

- ✿ Space research, dynamical systems, climate/ecological studies (carbon cycle+biomass), remote sensing (laser scanning, radar), biomedical imaging
- ✿ Generalized projection operators, phase-space tomography, Poincare inverse problem of dynamics, sparse stochastic tomography, optimal combination of multiple data modes (maximum compatibility estimate, MCE), information content of data
- ✿ TUT students from various fields, strongly application/hands-on oriented

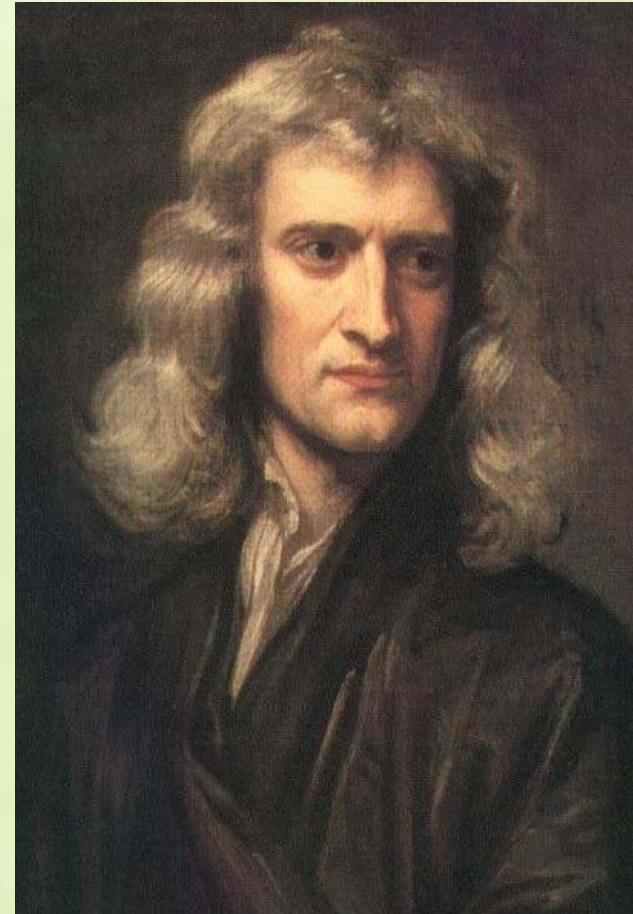
# Galaxies and dark matter

- ✿ We live at the edge of the disk
- ✿ Dust obscures a lot
- ✿ But high density of material: lots of data
- ✿ How is *dark matter* distributed?  
What is it made of?
- ✿ Thus: what potential field ( $\Rightarrow$  distribution of matter) holds the system together?



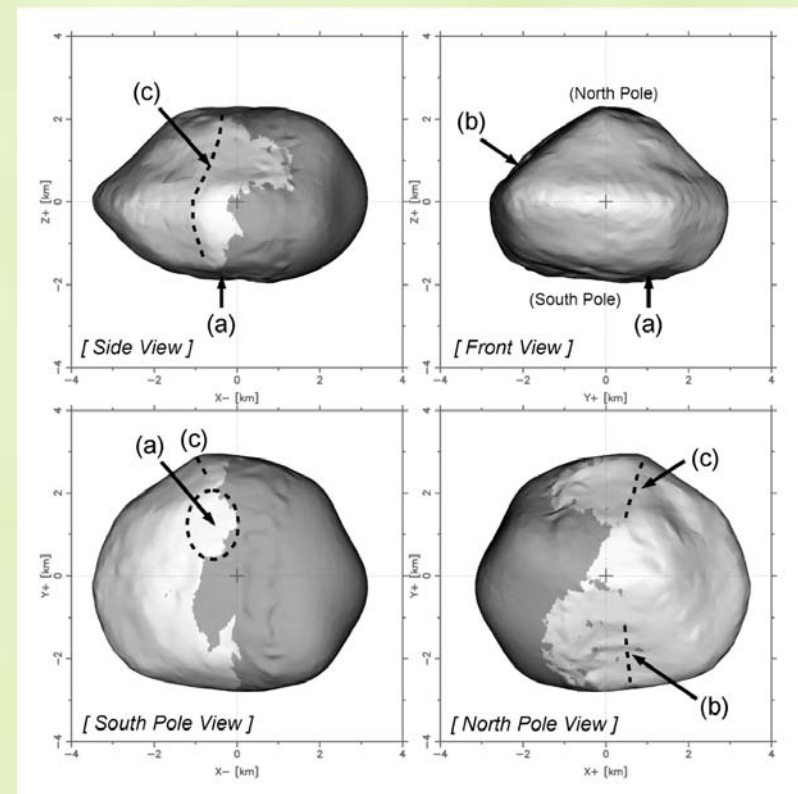
# Generalization of Newton's inverse problem

- ✿  $F \propto 1/r^2 \Rightarrow$  elliptic orbit (conical sections)
- ✿ Inverse problem: elliptic orbit  $\Rightarrow 1/r^2$  (when motion around foci)
- ✿ How to generalize this to  $N \gg 2$  bodies (e.g. positions and velocities of a billion stars)?
- ✿ Tomography in six dimensions!
- ✿ Poincare IP of dynamics: torus construction



# Space research: how to see the dark side

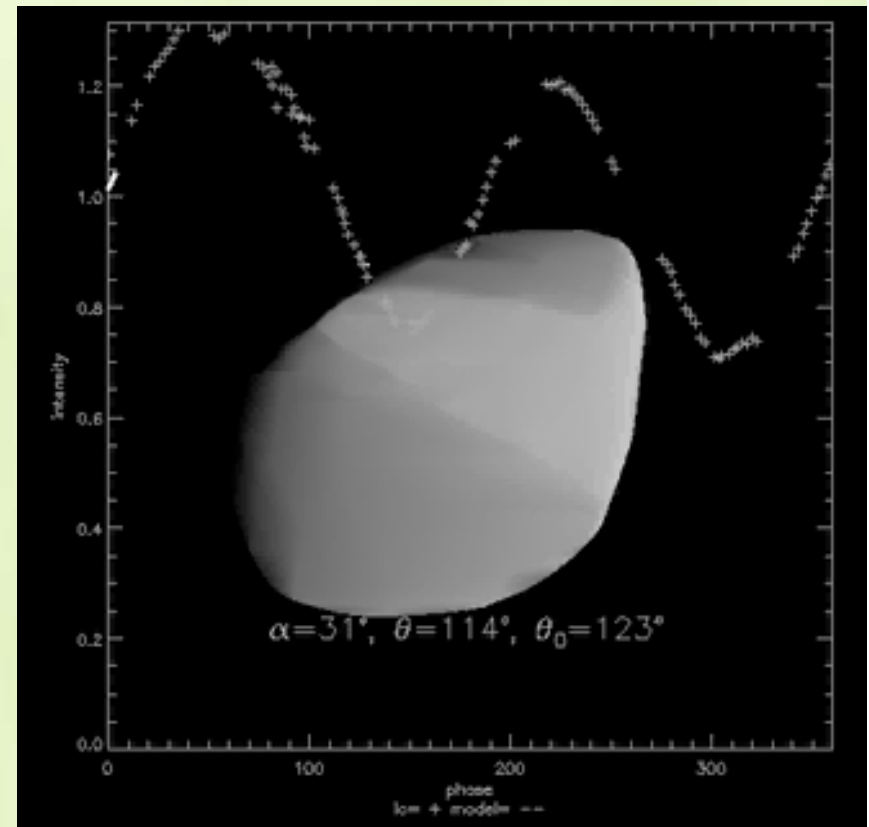
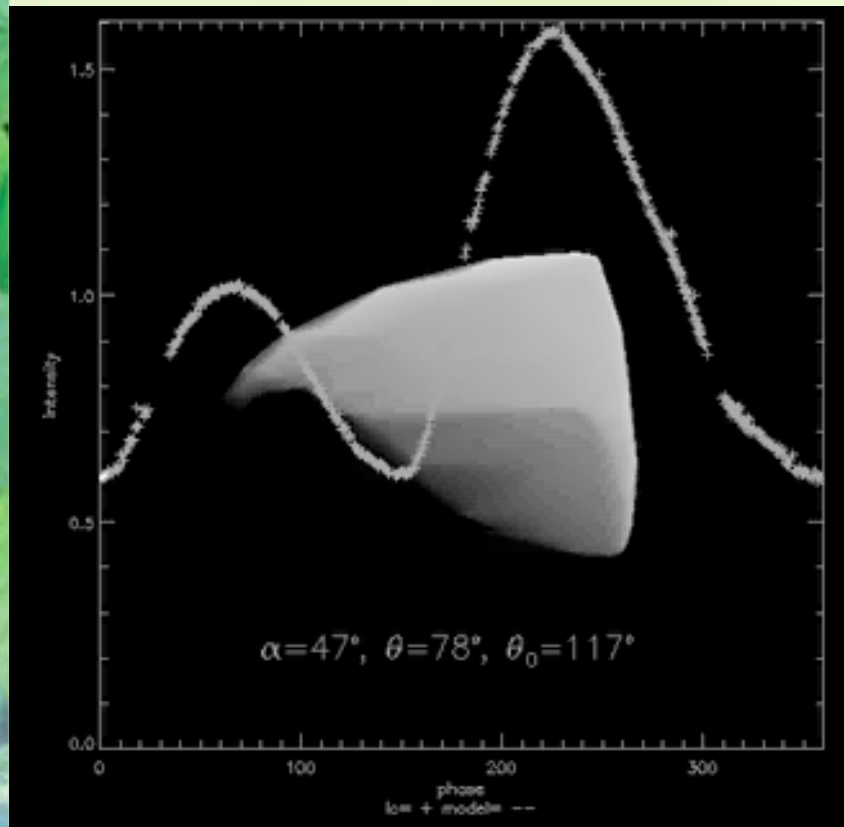
- ✿ ESA's Rosetta probe flew fast by the asteroid Steins and saw only one side (and the hi-res camera was lost)
- ✿ We reconstructed the other half from brightness data
- ✿ Stable solution: strong constraints by images
- ✿ YORP effect visible, cf. Kaasalainen et al. 2007, Nature



# Rosetta: Steins flyby

- ✿ Flyby lasted only 7 minutes
- ✿ Closest encounter 800 km, target size 5 km
- ✿ Speed w.r.t. target 8.6 km/s = 31000 km/h
- ✿ Dark side reconstruction cost ~0 €, gave significant added value to a project of 700 million €
- ✿ Keller et al., Science 2010 (Osiris team, ~50 co-authors)





- ✿ Shape/spin reconstruction methods now standard software (web+Windows) in international use; web-based database (maintained by J. Durech, Charles Univ., Prague)
- ✿ Now combining multiple data modalities (e.g. photometry and adaptive optics)

# Fundamental theorems

✿ Uniqueness theorem:  
With  $S^2 \times S^2$  data, i.e.,  
outside Russell  
degeneracy, there is a  
unique convex shape  
solution (corollary from  
Gaussian image  
uniqueness theorem  
and Minkowski-  
Nirenberg shape  
theorem)

✿ Stability theorem:  
the map  $LC \rightarrow \text{shape}$   
is continuous in  
usual topologies  
(the inverse  
problem is well-  
posed in the sense  
of Tikhonov)  $\Rightarrow$   
*Minkowski stability*



# Laboratory ground truth

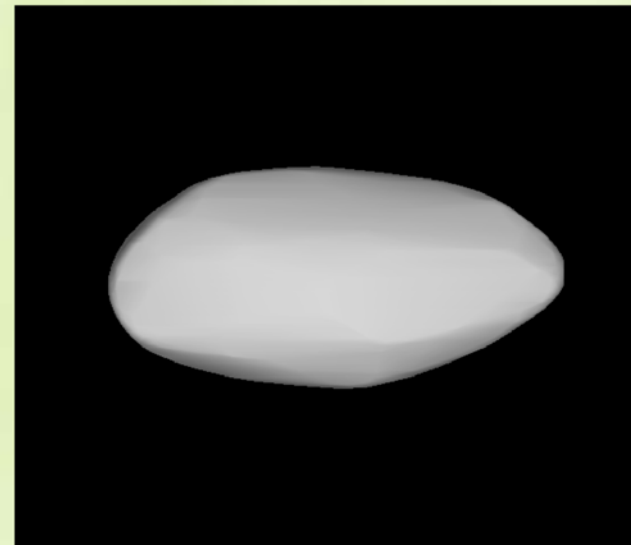
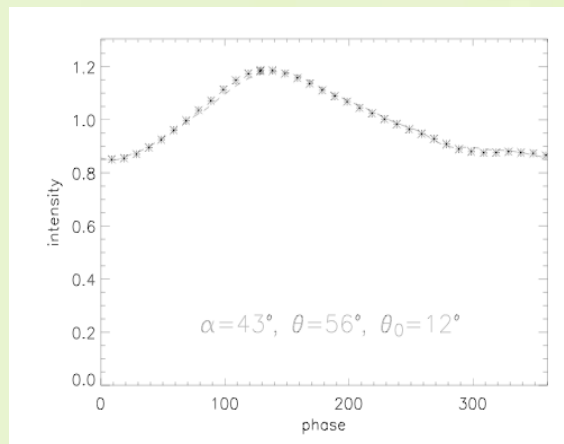
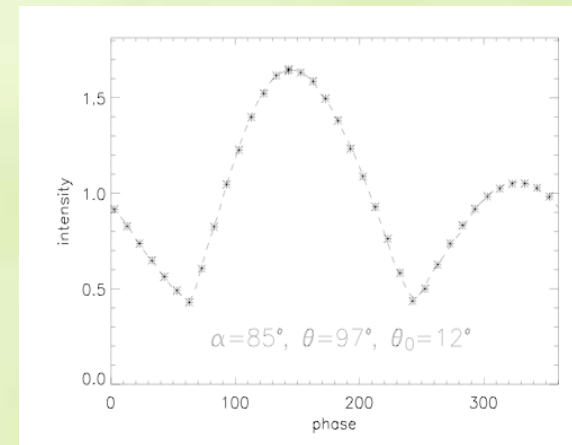
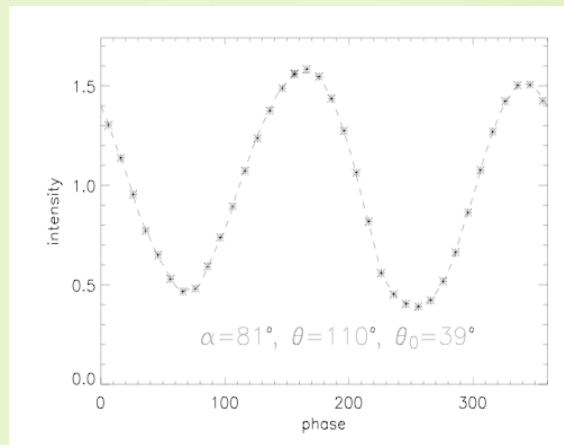




Fig. 5. Views of the target from the same viewpoints as the model images (Fig. 4).

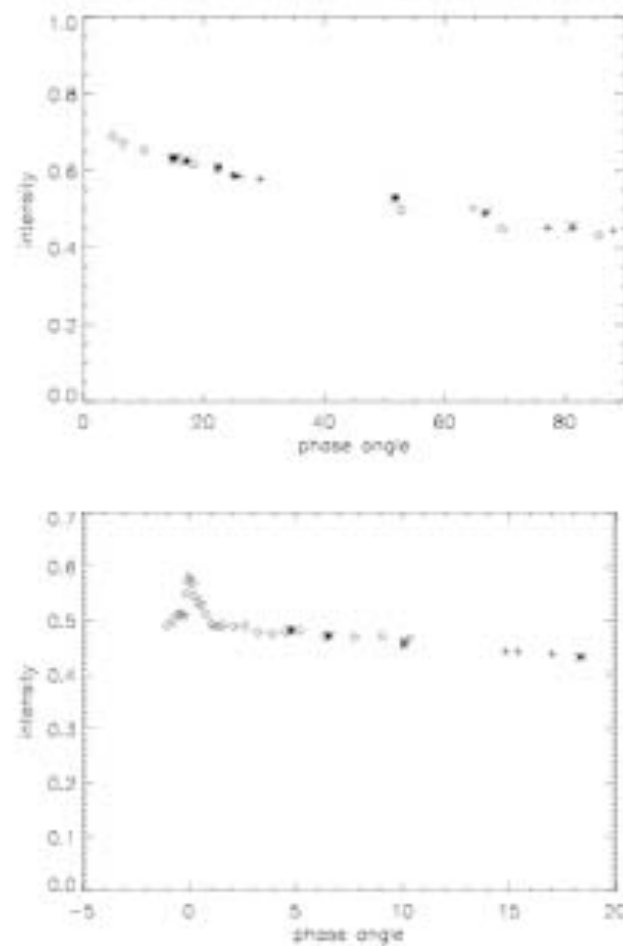


Fig. 7. a) The measured BRDFs at different values of  $\mu$ , at 633 nm. b) Phase curves at 633 nm combined (by normalizing at  $6.5^\circ$ ) from BRDF measurements (asterisk; the plot is made at  $\mu = 60^\circ$ ) and small-angle laser measurement (diamond).

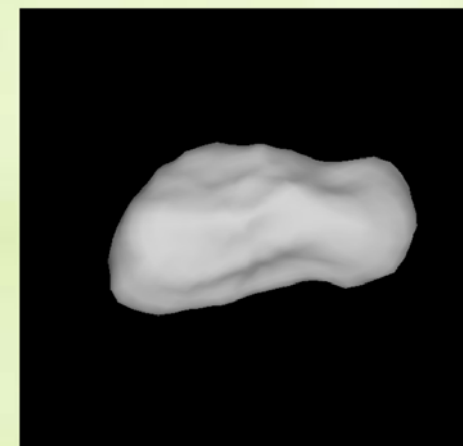
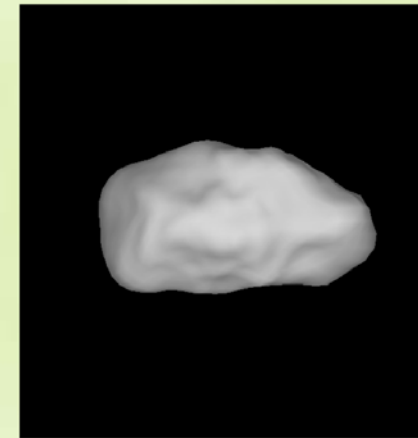
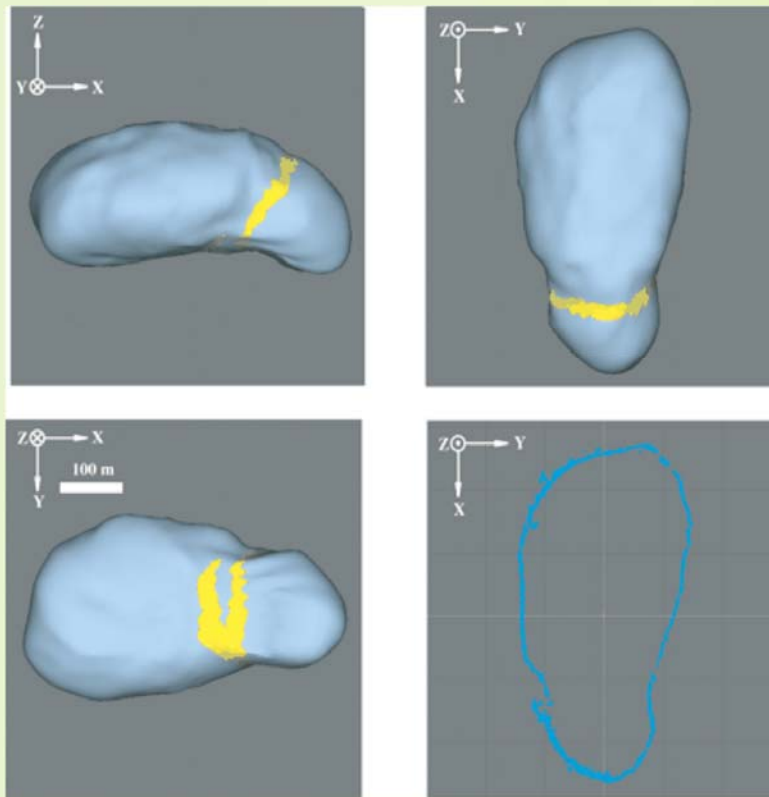
# Radars



- ✿ Sodankylä EISCAT 32 m
- ✿ Arecibo 300 m
- ✿ Ionosphere, space debris, moon, asteroids
- ✿ New EISCAT in planning
- ✿ Analysis in time/amplitude domain (vs. frequency/power)

# Caveat emptor: ground truth vs. basic radar model

Proper inverse modelling and model error analysis needed!



# Carbon cycle, biomass estimation+carbon footprint

- ✿ Collaboration with environmental and geodetic institutes
- ✿ Model selection problem, design of experiments
- ✿ Biomass estimation, disintegration profiles
- ✿ Laser scanning technologies, mobile platforms?

