## Solution 1

(a) summary statistics


| Categories | mean | standard deviation | sample size |
| :--- | ---: | ---: | ---: |
| novelist | 71.44776 | 13.05151 | 67 |
| poet | 63.18750 | 17.29710 | 32 |
| nonfiction writer | 76.875 | 14.09691 | 24 |

(b) Assumptions: Populations are normal with the same standard deviation.
(c) ANOVA
$H_{0}: \mu_{N O V}=\mu_{P}=\mu_{N F}$
$H_{a}$ : population mean are not all equal.

ANOVA table and F statistic

|  | SS | DF | MS | F |
| :--- | ---: | ---: | ---: | ---: |
| between the group | 2744.19 | 2 | 1372.10 | 6.56 |
| within the group | 25088.07 | 120 | 209.07 |  |
| Total | 27832.26 | 122 |  |  |

Since $F_{o b}>F_{.05}(2,120)=3.072$, we can reject $H_{0}$ at $5 \%$ level of significance and conclude that the mean age of death for different groups of writers are not the same.
NOTE: If you cannnot find the exact $F$ value in the F table, find the value closest to the critical value. In this example you may find $F_{.05}(2,100)$.
(d)
$H_{0}: \mu_{P}=\frac{1}{2}\left(\mu_{N O V}+\mu_{N F}\right)$

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H_{a}: \mu_{P}<\frac{1}{2}\left(\mu_{N O V}+\mu_{N F}\right)
$$

T.S.

$$
\begin{aligned}
c & =a_{p} \bar{x}_{p}+a_{\text {nov }} \bar{x}_{n o v}+a_{n f} \bar{x}_{n f} \\
& =1 \times 63.19-0.5 \times 71.45-0.5 \times 76.88 \\
& =-11 \\
S E_{c} & =\sqrt{\mathrm{MSE}} \sqrt{\frac{a_{P}^{2}}{n_{P}}+\frac{a_{N O V}^{2}}{n_{N O V}}+\frac{a_{N F}^{2}}{n_{N F}}} \\
& =\sqrt{209.07} \sqrt{1 / 32+0.25 / 67+0.25 / 24} \\
& \approx=3.12 \\
t & =\frac{c}{S E_{c}}=\frac{-11}{3.12} \approx-3.51 \\
\nu & =120
\end{aligned}
$$

R.R. : Reject $H_{0}$ if $t<-t .05(120)=-1.658$

Conclusion: Since $t_{o b}<-1.658$, we can reject $H_{0}$ at $5 \%$ level of significance and conclude that poets die younger than novelist and nonfiction writers.

