Solution 1

(a) summary statistics



Categories	mean	standard deviation	sample size
novelist	$71.\ 44776$	13.05151	67
poet	63.18750	17.29710	32
nonfiction writer	76.875	14.09691	24

(b) Assumptions: Populations are normal with the same standard deviation.

(c) ANOVA

 $H_0: \mu_{NOV} = \mu_P = \mu_{NF}$

 H_a : population mean are not all equal.

ANOVA table and F statistic

	\mathbf{SS}	DF	MS	\mathbf{F}
between the group	$2\ 744.19$	2	$1\ 372.10$	6.56
within the group	$25\ 088.07$	120	209.07	
Total	$27 \ 832.26$	122		

Since $F_{ob} > F_{.05}(2, 120) = 3.072$, we can reject H_0 at 5% level of significance and conclude that the mean age of death for different groups of writers are not the same.

NOTE: If you cannot find the exact F value in the F table, find the value closest to the critical value. In this example you may find $F_{.05}(2, 100)$.

$$H_0: \mu_P = \frac{1}{2}(\mu_{NOV} + \mu_{NF})$$

 $H_a: \mu_P < \frac{1}{2}(\mu_{NOV} + \mu_{NF})$

T.S.

$$c = a_p \overline{x}_p + a_{nov} \overline{x}_{nov} + a_{nf} \overline{x}_{nf}$$

= 1 × 63.19 - 0.5 × 71.45 - 0.5 × 76.88
= -11
$$SE_c = \sqrt{\text{MSE}} \sqrt{\frac{a_P^2}{n_P} + \frac{a_{NOV}^2}{n_{NOV}} + \frac{a_{NF}^2}{n_{NF}}}$$

= $\sqrt{209.07} \sqrt{1/32 + 0.25/67 + 0.25/24}$
≈= 3.12
$$t = \frac{c}{SE_c} = \frac{-11}{3.12} \approx -3.51$$

 $\nu = 120$

R.R. : Reject H_0 if $t < -t_{.05}(120) = -1.658$ Conclusion: Since $t_{ob} < -1.658$, we can reject H_0 at 5% level of significance and conclude that poets die younger than novelist and nonfiction writers.