Every strongly rigid metric space $(X, d)$ has the following properties. Any two disjoint subsets of $X$ admit at most on best proximity pair. For every proximinal subset $A$ of $X$ each point of $X$ has exactly one best approximation in $A$. The symmetric group of $X$ coincides with the group of all combinatorial self-similarities of $(X, d)$. The main goal is to characterize, up to isometry, those semimetric spaces that have these properties. This talk is based on the joint works with Viktoriia Bilet and Ruslan Shanin.

