Every strongly rigid metric space (X, d) has the following properties. Any two disjoint subsets of X admit at most on best proximity pair. For every proximinal subset A of X each point of X has exactly one best approximation in A. The symmetric group of X coincides with the group of all combinatorial self-similarities of (X, d). The main goal is to characterize, up to isometry, those semimetric spaces that have these properties. This talk is based on the joint works with Viktoriia Bilet and Ruslan Shanin.