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*The maximal operator, weights and extrapolation on variable Lebesgue spaces*

The variable Lebesgue spaces are a generalization of the classical  $L^p$  spaces, replacing the constant exponent  $p$  with a function  $p(\cdot)$ . We will discuss recent work to establish a theory of weighted norm inequalities on these spaces, primarily by extending the theory of Rubio de Francia extrapolation to this setting. This requires a good understanding of the Hardy-Littlewood maximal operator. If time allows, we will also discuss work on the structure of  $A_p$  weights in the variable exponent setting, an area where a great deal of work remains to be done.