

# **Astrophysical light scattering problems (PAP316)**

## **Lecture 4b**

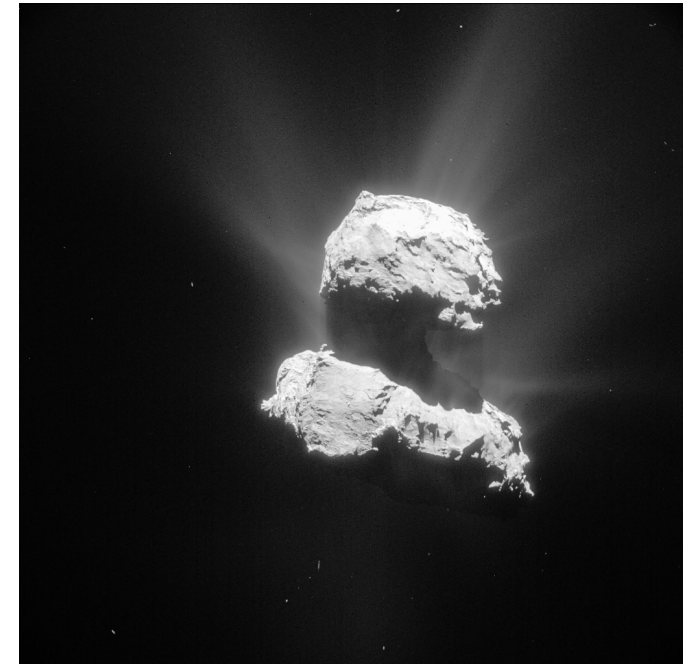
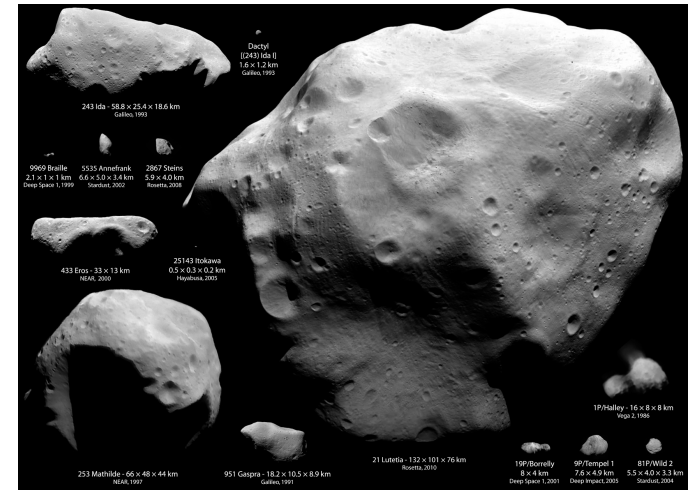
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# Introduction

- Inverse problem solutions powered by simplified scattering modeling
- Phenomenological scatterer
  - Mathematical model for the scattering phase matrix
  - Retrieval of parameters from observed/measured scattering characteristics
  - Physics-based interpretation of the resulting phase matrix
  - Reference: Muinonen & Videen, JQSRT 113, 2385, 2012

# Spherical particles measured

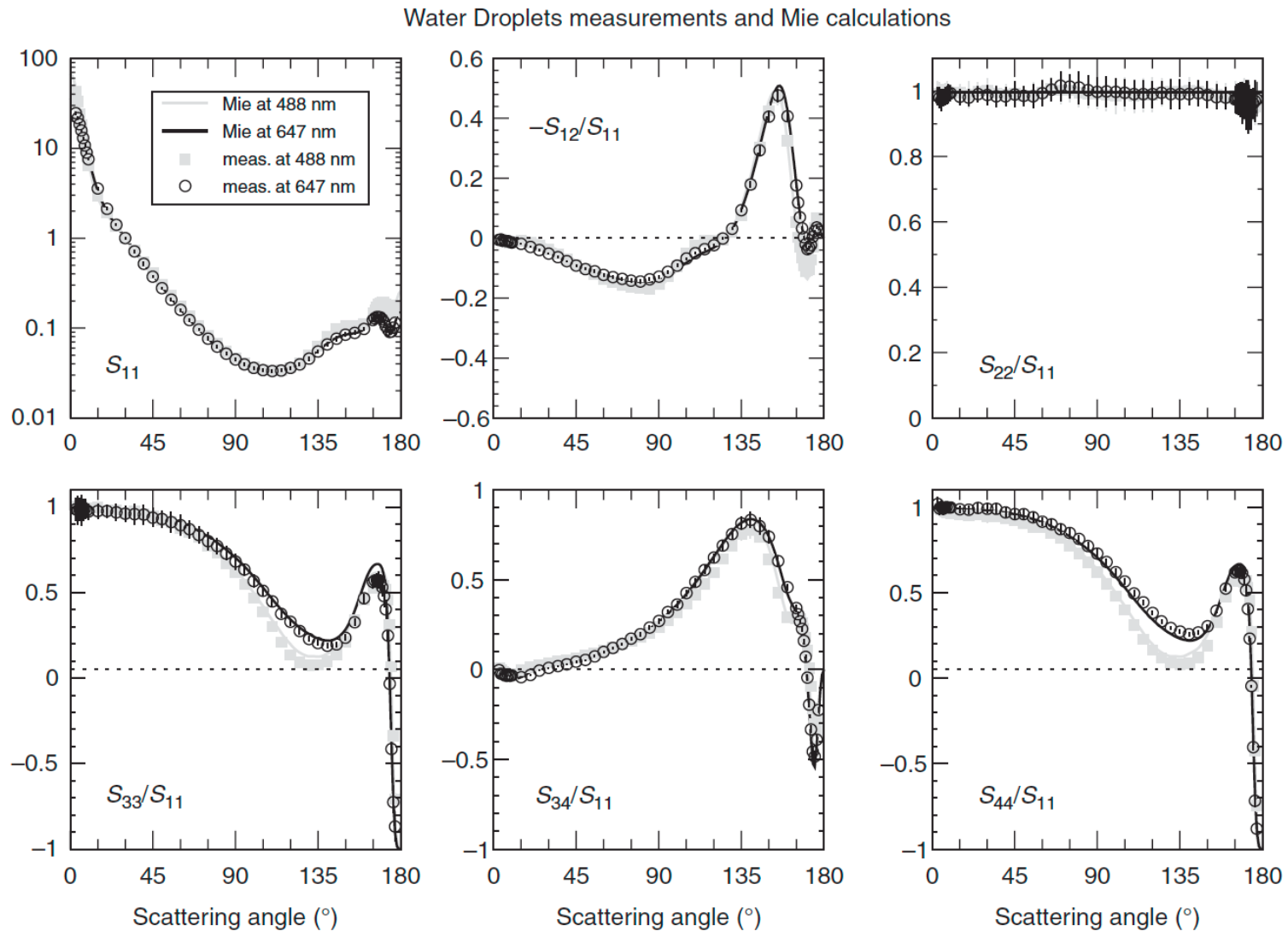


FIGURE 8.3 Comparison of Lorenz-Mie calculations and measured scattering matrix elements for a size distribution of water droplets. The measurements are performed at 488 nm (gray symbols) and 647 nm (black symbols). The  $S_{11}$  element is normalized to  $I$  at  $30^\circ$ .

# Olivine particles measured

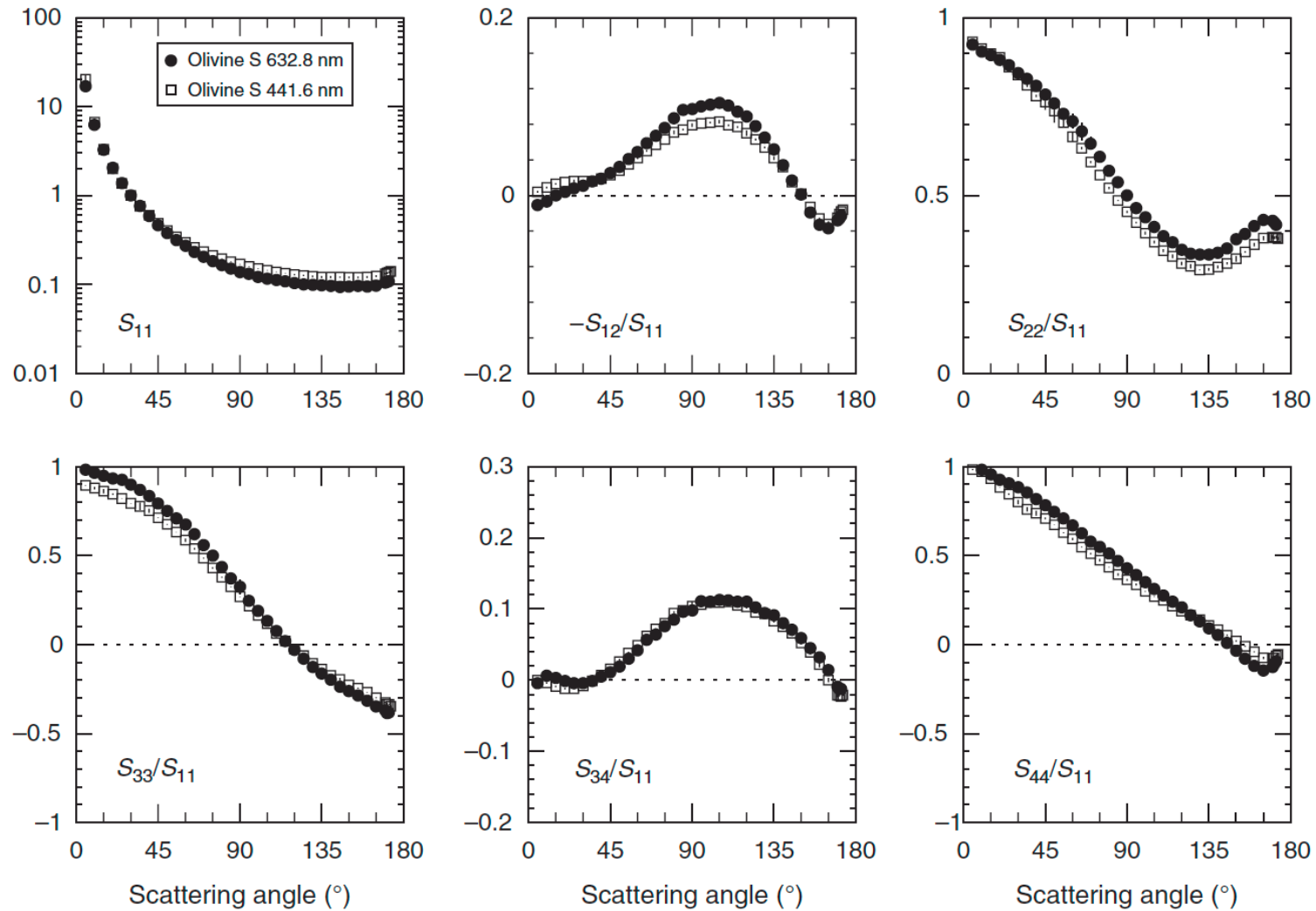


FIGURE 8.7 Measured scattering matrix elements as functions of the scattering angle for a magnesium-rich olivine sample (Olivine S in Muñoz *et al.* 2000). Filled circles and squares correspond to the measurements at 632.8 nm and 441.6 nm, respectively.

# Phenomenological scatterer

$$\mathbf{P}(\theta) \propto P_{11}(\theta)[w_+ \mathbf{M}_+(\theta) + w_- \mathbf{M}_-(\theta)], \quad w_+ + w_- = 1$$

$$\mathbf{M}_\pm(\theta) = \begin{pmatrix} 1 & \mp \frac{\sin^2 \theta_\pm}{1 + \cos^2 \theta_\pm} & 0 & 0 \\ \mp \frac{\sin^2 \theta_\pm}{1 + \cos^2 \theta_\pm} & 1 & 0 & 0 \\ 0 & 0 & \frac{2 \cos \theta_\pm}{1 + \cos^2 \theta_\pm} & 0 \\ 0 & 0 & 0 & \frac{2 \cos \theta_\pm}{1 + \cos^2 \theta_\pm} \end{pmatrix}.$$

For  $e_+ = e_- = 0$ ,  $\theta_+ = \theta_- = \theta$  and the normalized weight factors

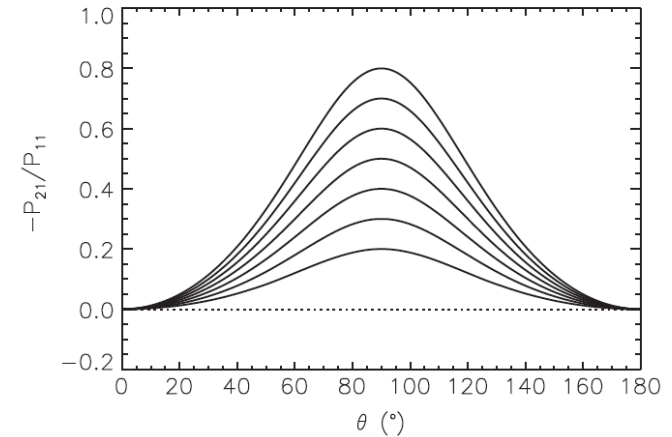
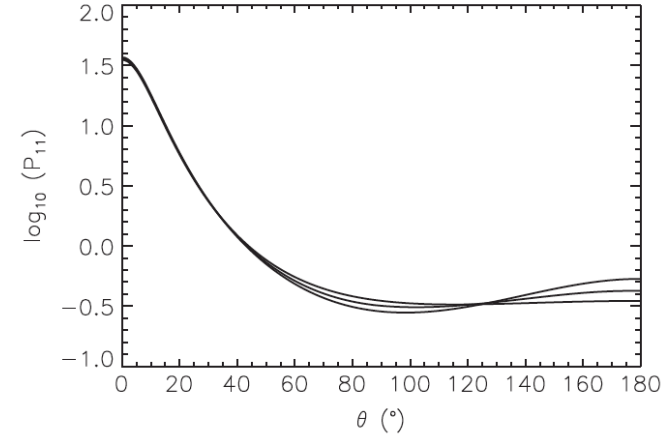
$$w_+ = \frac{1}{2}(1 + P_{\max}),$$

$$w_- = \frac{1}{2}(1 - P_{\max}), \quad (4)$$

where  $P_{\max}$  gives the maximum for the degree of linear polarization  $-P_{12}/P_{11}$  at  $\theta = 90^\circ$ .

$$P_{11}(\theta) = w \frac{1 - g_1^2}{(1 + g_1^2 - 2g_1 \cos \theta)^{3/2}} + (1 - w) \frac{1 - g_2^2}{(1 + g_2^2 - 2g_2 \cos \theta)^{3/2}},$$

$$g = wg_1 + (1 - w)g_2, \quad w = \frac{g - g_2}{g_1 - g_2},$$

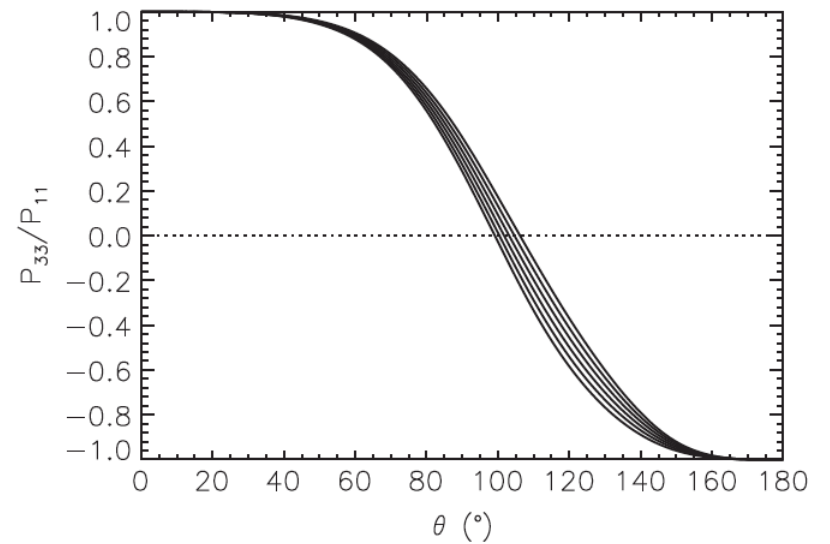
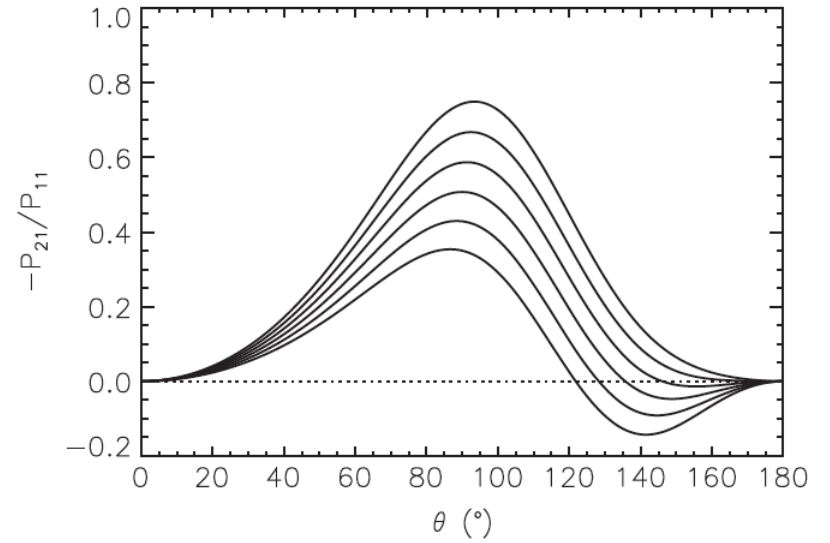


**Fig. 1.** Double Henyey–Greenstein single-scattering phase function  $P_{11}$  (top) and scaled Rayleigh degree of linear polarization for unpolarized incident light  $-P_{12}/P_{11}$  (bottom). For the phase functions  $P_{11}$ , the total asymmetry parameter is  $g=0.6$  and the forward asymmetry is  $g_1 = 0.8$ , whereas, in the order of increasing backscattering, the backward asymmetry assumes the values  $g_2 = -0.1, -0.2, \text{ and } -0.3$ . For the polarizations  $-P_{12}/P_{11}$ , the maximum polarization assumes the values  $P_{\max} = 0.2, 0.3, \dots, 0.8$ . In addition,  $P_{22} = P_{11}$ ,  $P_{33}/P_{11} = P_{44}/P_{11} = \cos \theta$ , and  $P_{34} = -P_{43} = 0$ .

$$\theta_+ - e_+ \sin \theta_+ = \theta,$$

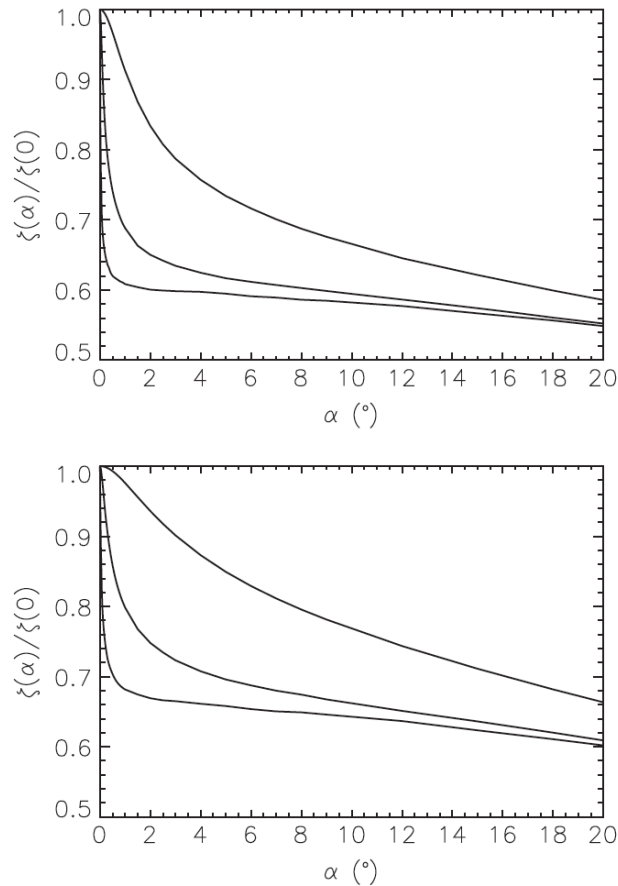
$$\theta_- - e_- \sin \theta_- = \theta.$$

seven parameters:  $\tilde{\omega}$ ,  $g$ ,  $g_1$ ,  $g_2$ ,  $w_+$ ,  $e_+$ ,  
and  $e_-$ .

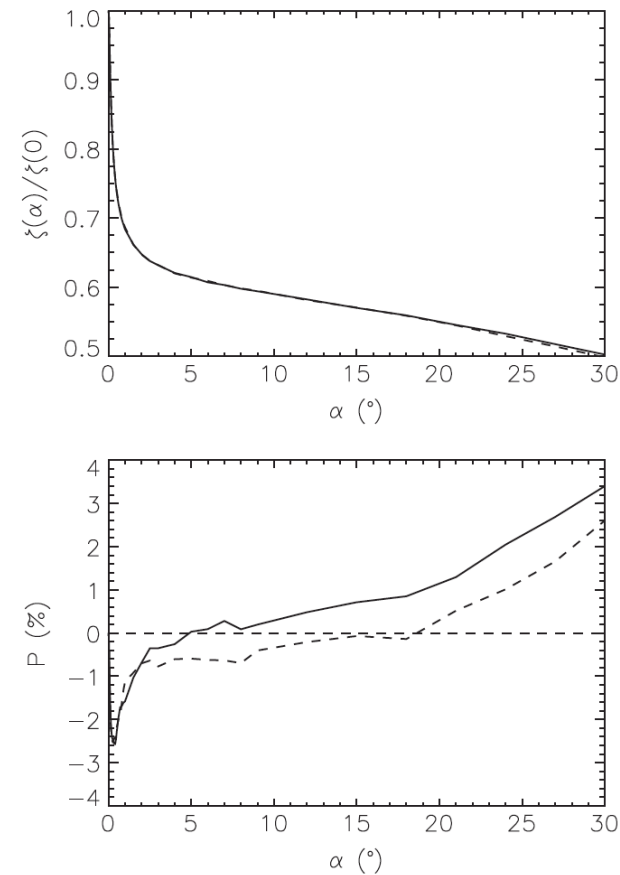


**Fig. 2.** Degree of linear polarization  $-P_{12}/P_{11}$  (top) and  $P_{33}/P_{11}$  (bottom) for example negatively polarizing single scatterers. The eccentricities are  $e_+ = -0.1$  and  $e_- = -0.6$  and the weights are  $w_+ = 1 - w_- = 0.60, 0.65, 0.70, \dots, 0.85$ . With increasing  $w_+$ , the polarization  $-P_{12}/P_{11}$  increases and  $P_{33}/P_{11}$  moves to the left.

# Multiple scattering computations

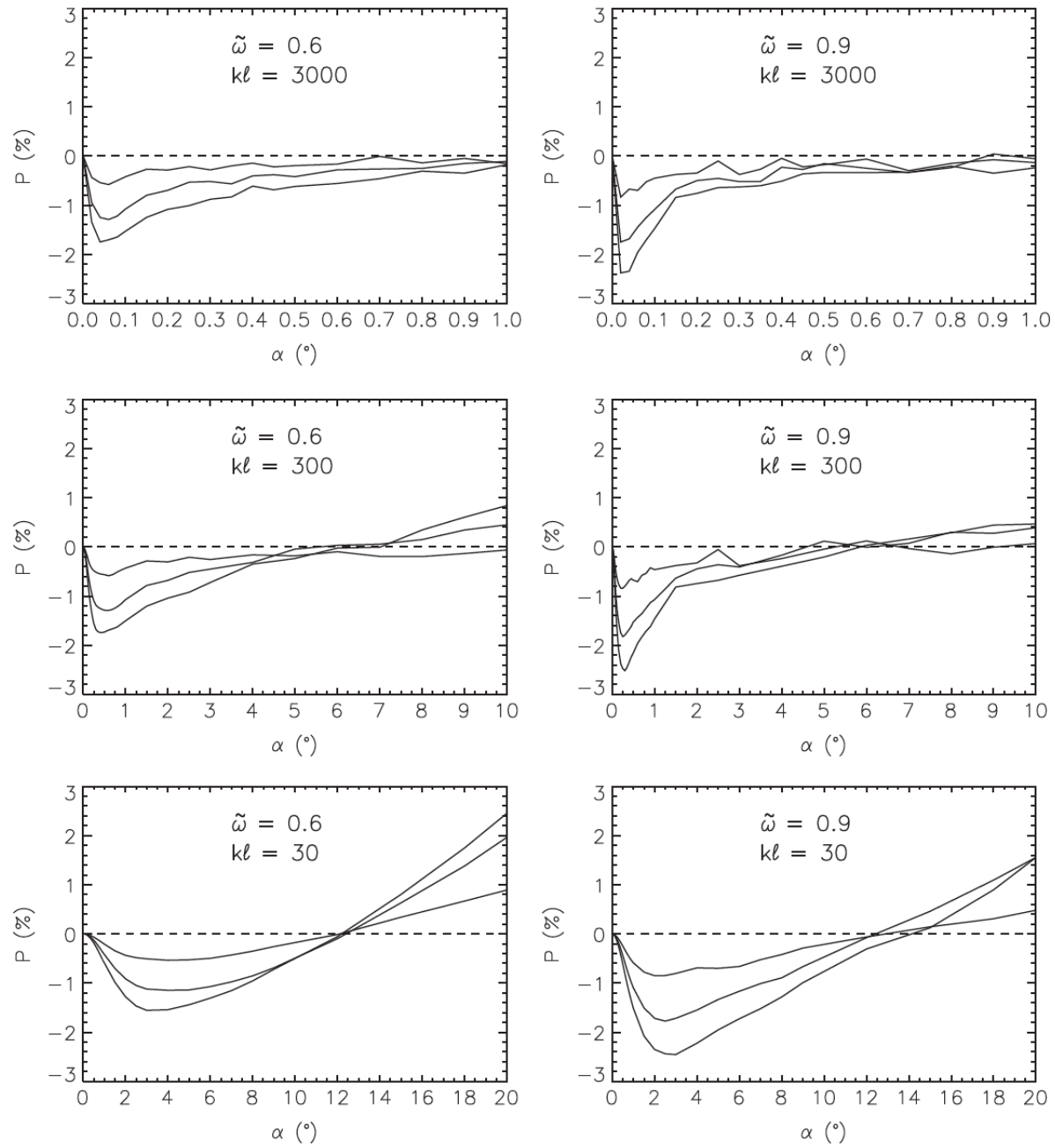


**Fig. 3.** Coherent-backscattering enhancement factors computed using phenomenological single scatterers with single-scattering albedo  $\bar{\omega} = 0.9$  (top) and  $0.6$  (bottom) for  $k\ell = 30, 300,$  and  $3000$  (large, intermediate, and small angular widths, respectively). In these examples, polarization in single scattering (here  $P_{\max} = 0.6$ ) has a minor effect on the enhancement factors.



**Fig. 5.** Enhancement factors (top) and degrees of linear polarization (bottom) computed using phenomenological single scatterers with  $\bar{\omega} = 0.9$  and  $w_+ = 1 - w_- = 0.8$ . The eccentricities are  $e_+ = -0.1$  and  $e_- = -0.6$  (solid line; neutral single-scatterer polarization near backscattering) as well as  $e_+ = -0.1$  and  $e_- = -0.8$  (dashed line; negative single-scatterer polarization near backscattering). The mean free path is  $k\ell = 300$ .





**Fig. 4.** Degrees of linear polarization for unpolarized incident radiation for  $\tilde{\omega} = 0.6$  (left) and  $0.9$  (right) in the case of  $kl = 30$  (bottom),  $300$  (middle), and  $3000$  (top). The eccentricities  $e_+ = e_- = 0$  and the maximum polarization assumes the values  $P_{\max} = 0.2, 0.4,$  and  $0.6$  (shallow, intermediate, and pronounced patterns, respectively).

# Example: Jovian moon Europa

Kiselev et al.,  
unpublished

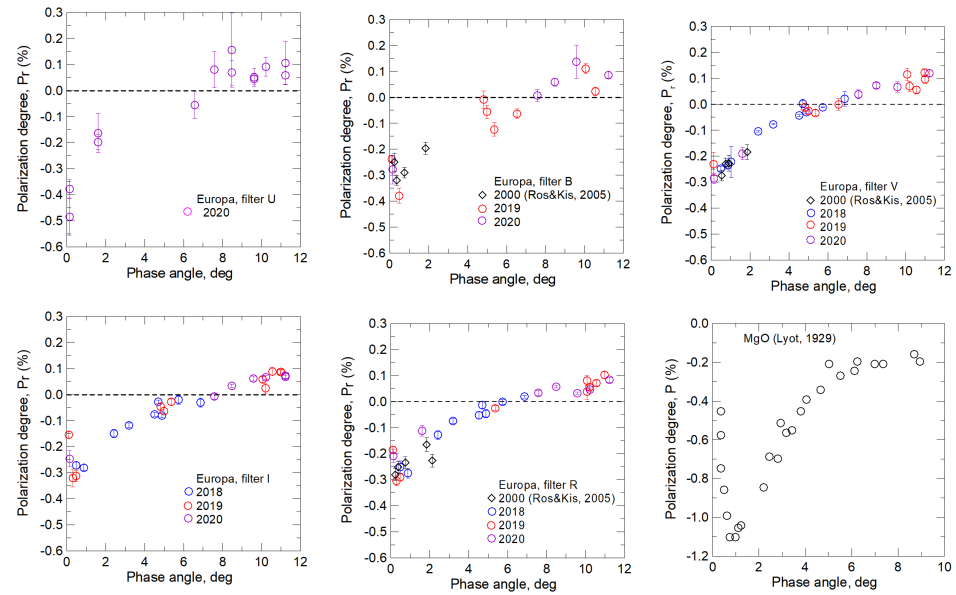


Fig. 2. Phase-angle polarization dependences for Jupiter’s satellite Europa in the *UBVRI* filters, obtained in 2018–2020 (open circles) and in 2000 (Rosenbush and Kiselev, 2005) (diamonds). For comparison (bottom row, right panel), the results of laboratory measurements of the polarization of MgO are presented (adopted from the paper by Lyot, 1929).

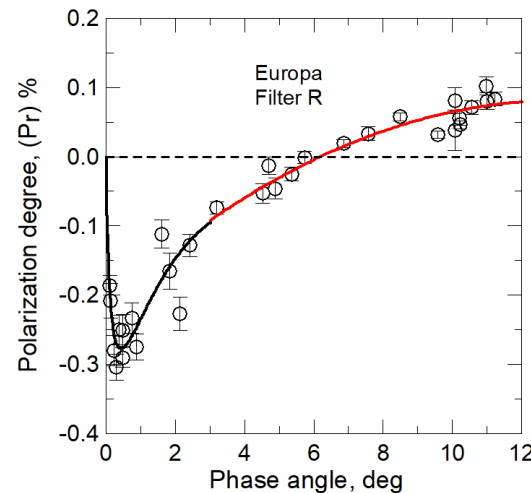
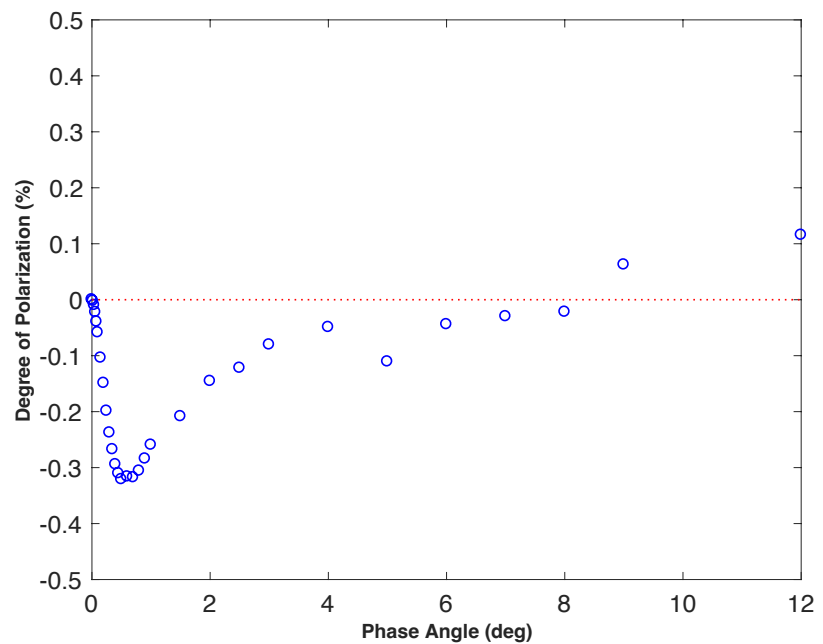
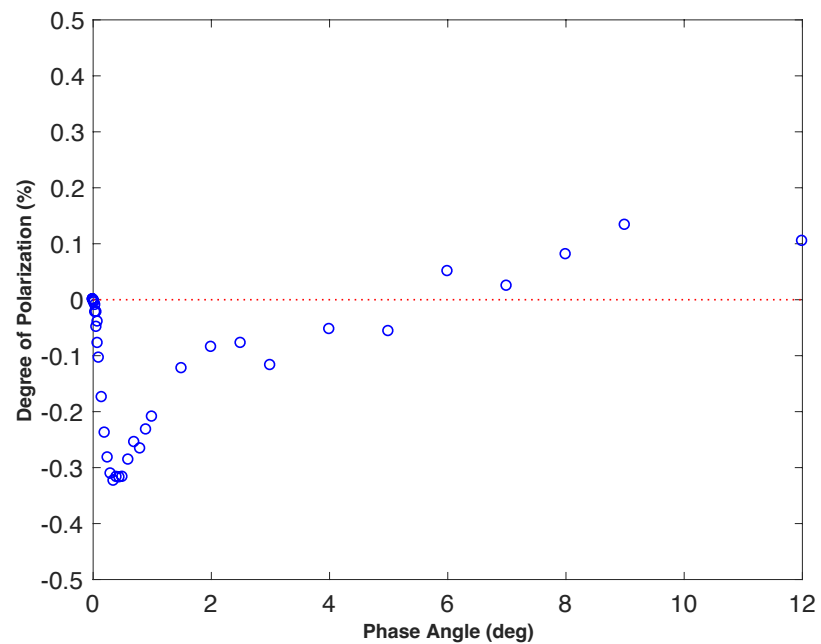


Fig. 3. The fits of Europa’s data in the *R* filter taken from Table 4 and Rosenbush&Kiselev 2005). The black curve is an approximation of data in the phase angle interval  $\approx(0^\circ - 3^\circ)$  with expression (7), while the red curve is the fitting of data in the phase angle interval  $\approx(3^\circ - 12^\circ)$  with a second-degree polynomial.

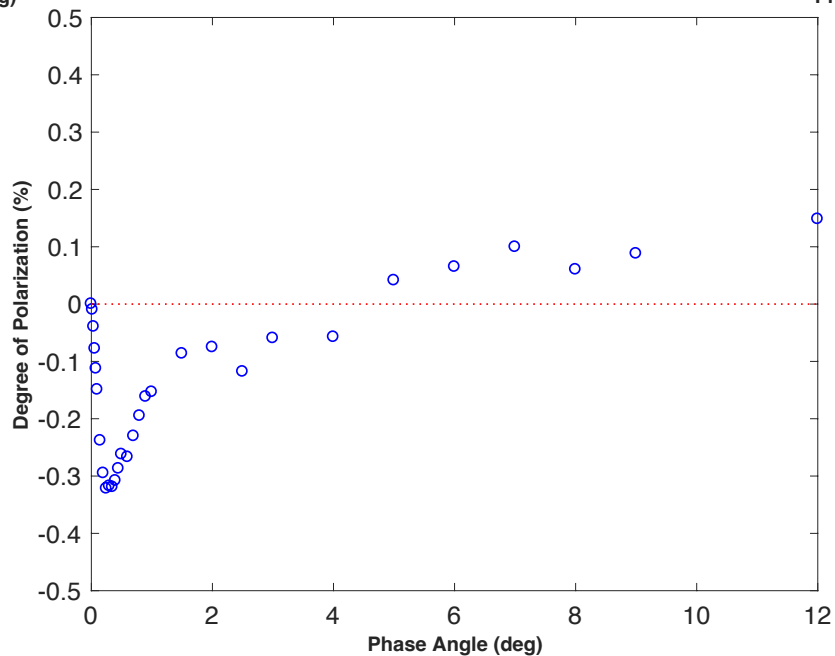
**kl = 100**



**kl = 150**



**kl = 200**



**$\omega = 0.984$**   
 **$P_{\max} = 0.08$**   
 **$g = 0.6$**   
 **$g_1 = 0.8$**   
 **$g_2 = -0.1$**   
**( $p = 0.67-0.68$ )**

# Intermediate conclusions

- Extension to measured scattering phase matrices
- Application at large