

# Computational light scattering (PAP315)

## Lecture 1

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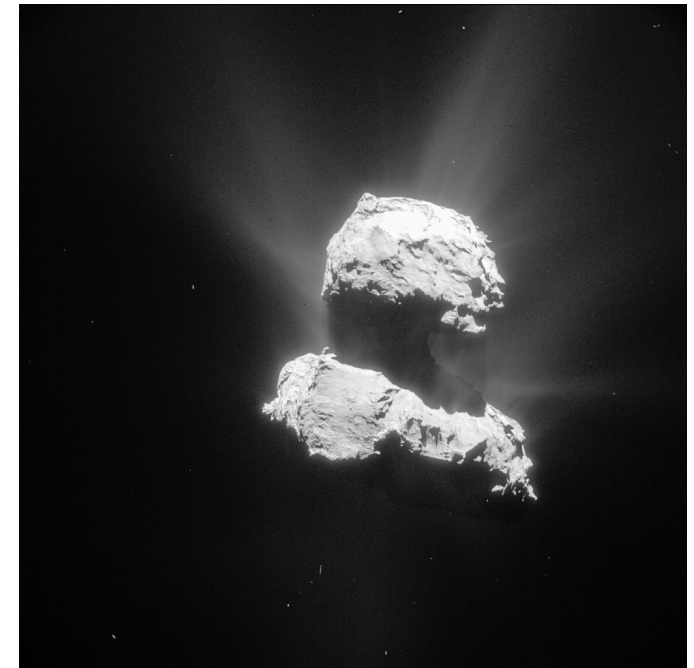
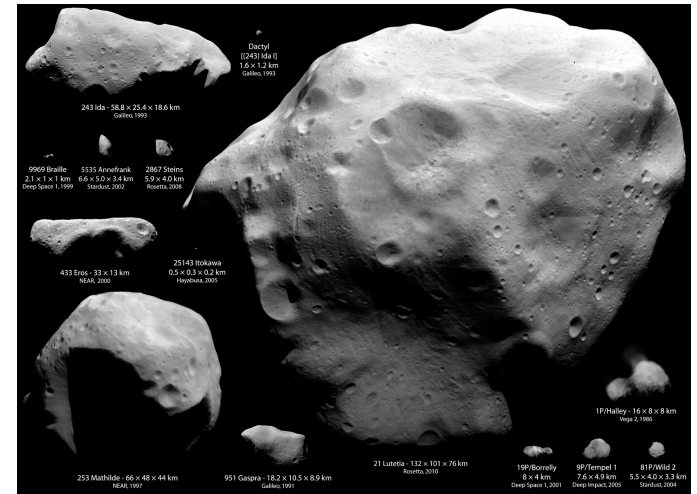
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# Introduction

- Physical characterization of the **surfaces** of **airless planetary objects**
- **Direct problem** of light scattering by **discrete random media** of particles with **varying particle size, shape, refractive index, and volume density**
- **Inverse problem** based on **astronomical observations and/or experimental measurements**
- **Plane of scattering, scattering angle, solar phase angle, degree of linear polarization**



243 Ida - 58.8 × 25.4 × 18.6 km  
Galileo, 1993

Dactyl  
[[243) Ida I]  
1.6 × 1.2 km  
Galileo, 1993



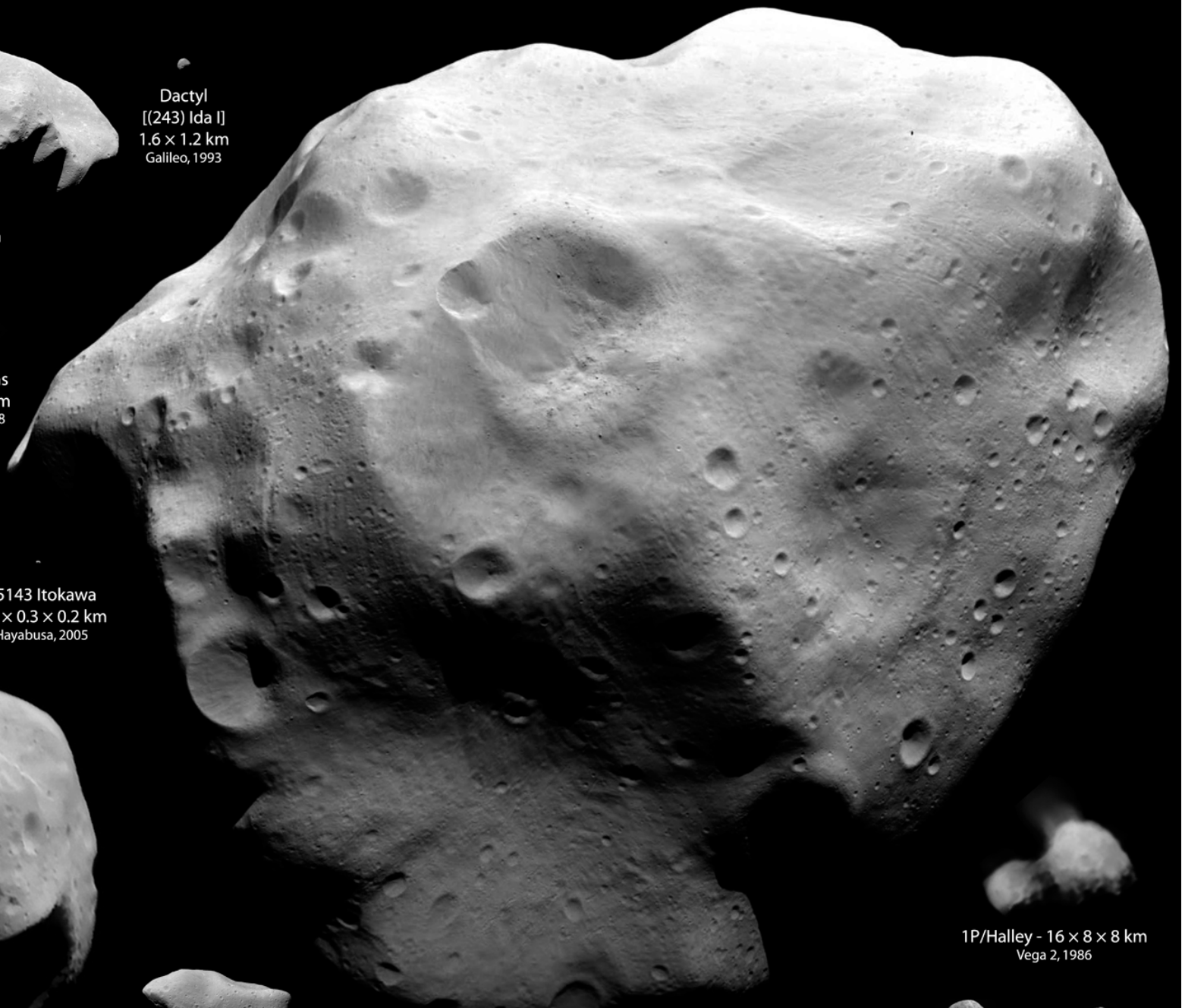
9969 Braille  
2.1 × 1 × 1 km  
Deep Space 1, 1999

5535 Annefrank  
6.6 × 5.0 × 3.4 km  
Stardust, 2002

2867 Steins  
5.9 × 4.0 km  
Rosetta, 2008



433 Eros - 33 × 13 km  
NEAR, 2000



25143 Itokawa  
0.5 × 0.3 × 0.2 km  
Hayabusa, 2005

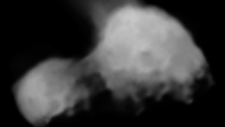


253 Mathilde - 66 × 48 × 44 km  
NEAR, 1997



951 Gaspra - 18.2 × 10.5 × 8.9 km  
Galileo, 1991

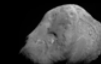
21 Lutetia - 132 × 101 × 76 km  
Rosetta, 2010



1P/Halley - 16 × 8 × 8 km  
Vega 2, 1986



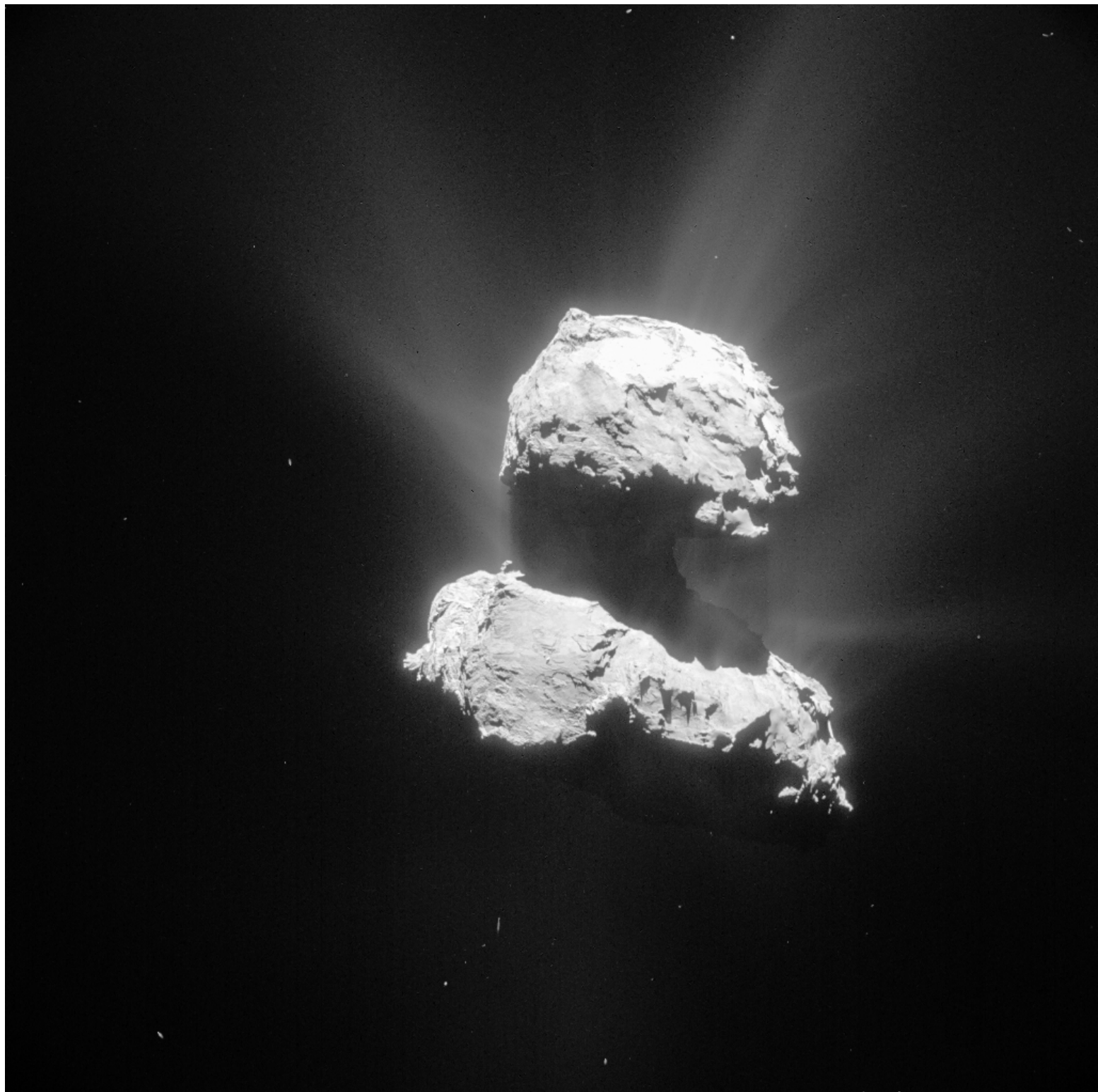
19P/Borrelly  
8 × 4 km  
Deep Space 1, 2001



9P/Tempel 1  
7.6 × 4.9 km  
Deep Impact, 2005



81P/Wild 2  
5.5 × 4.0 × 3.3 km  
Stardust, 2004



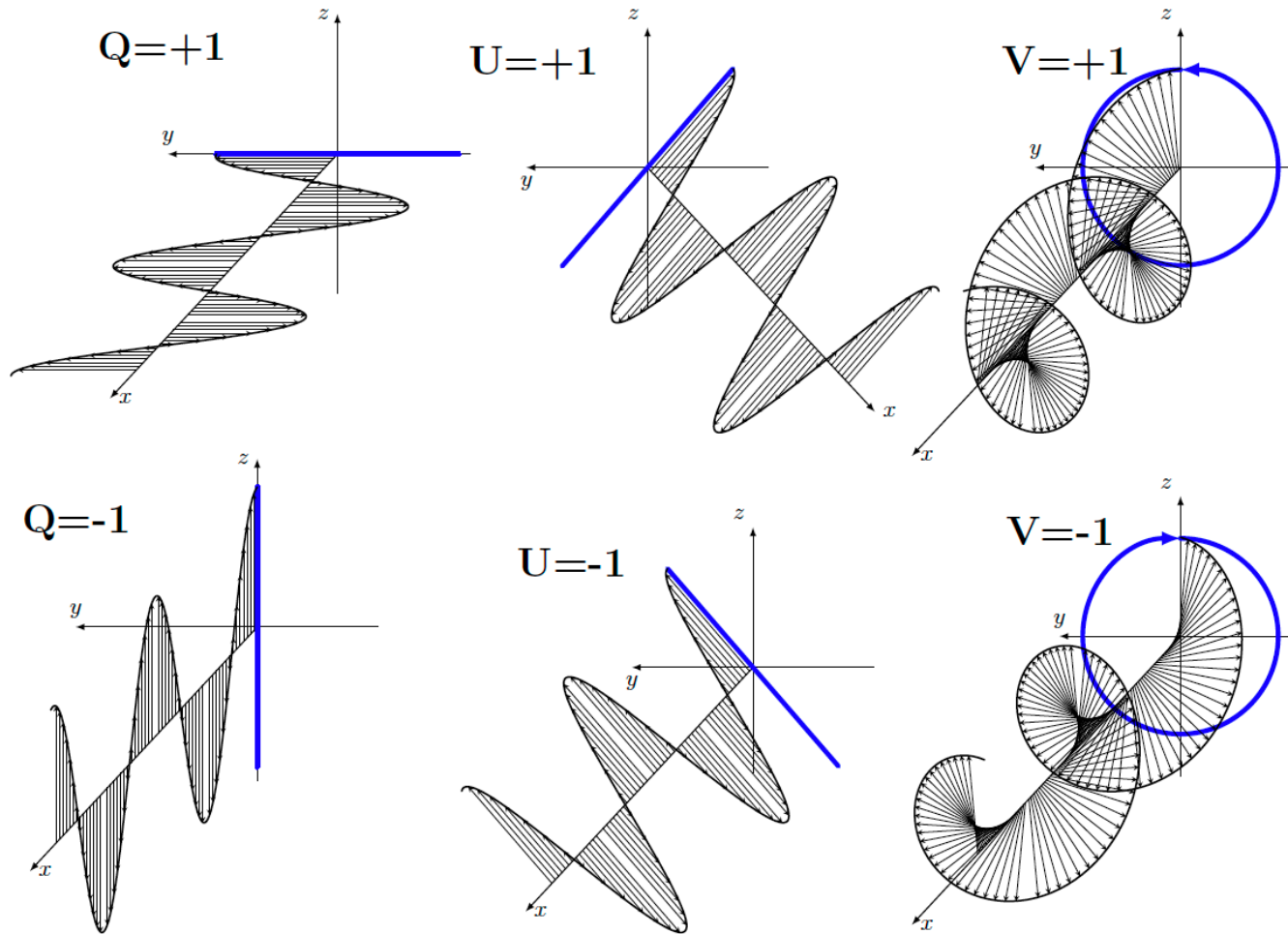


Figure 2.1: Stokes parameters explained visually by drawing the plane of propagation. While  $Q$  and  $U$  propagate in a plane, the plane of  $V$  rotates and thus has a circular pattern. The sign controls the orientation of the plane, whereas intensity  $I$  defines the amplitude of the oscillation. For a visual aid,  $U=-1$  propagates in the same direction as  $U=+1$ , but the  $x$ -axis is shifted to make the pattern more distinctive.

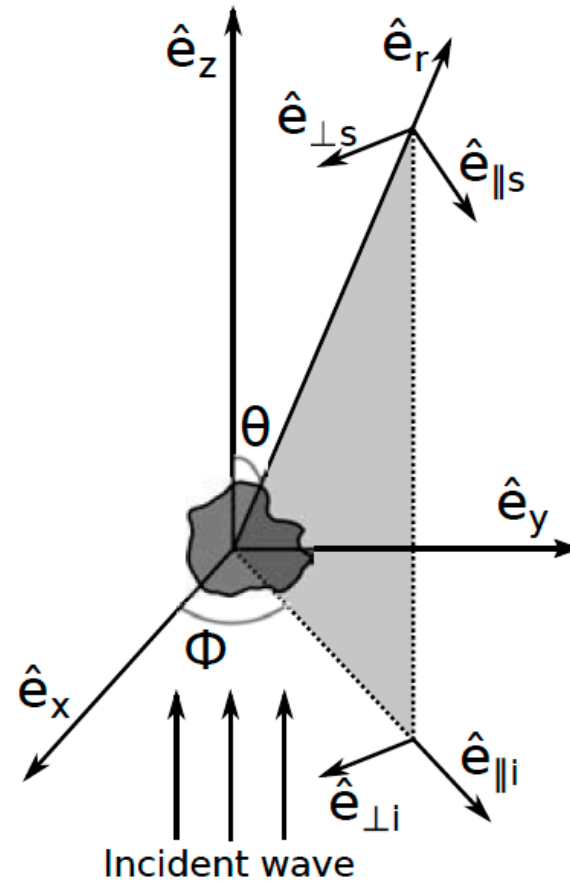


Figure 2.2: Illustration of the incident wave and the scattering plane. (Bohren and Huffman, 1983)

$$\begin{aligned}
 I &\propto E_{\parallel} E_{\parallel}^* + E_{\perp} E_{\perp}^* \\
 Q &\propto E_{\parallel} E_{\parallel}^* - E_{\perp} E_{\perp}^* \\
 U &\propto E_{\parallel} E_{\perp}^* + E_{\perp} E_{\parallel}^* \\
 V &\propto i(E_{\parallel} E_{\perp}^* - E_{\perp} E_{\parallel}^*)
 \end{aligned}$$

$I$  = intensity

$Q$  and  $U$  = the degree and direction of linear polarization

$V$  = the degree and handedness of the circular polarization.

$$\sqrt{Q^2 + U^2 + V^2} / I = \text{degree of polarization}$$

$$\sqrt{Q^2 + U^2} / I = \text{degree of linear polarization}$$

$$V / I = \text{degree of circular polarization}$$



With Stokes parameters, we obtain the 4×4 Mueller matrix form for the scattering equation:

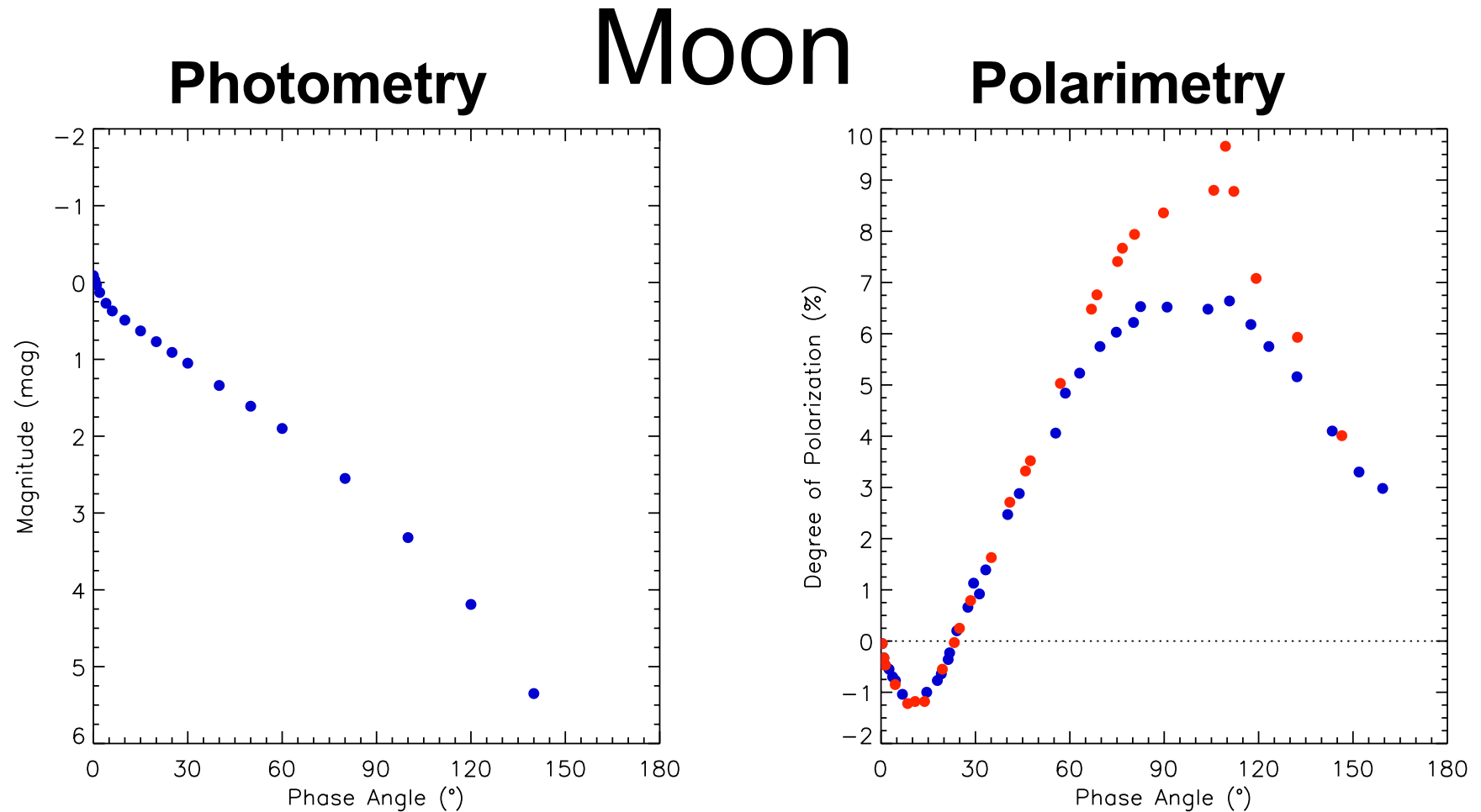
$$\begin{pmatrix} I_s \\ Q_s \\ U_s \\ V_s \end{pmatrix} = \frac{C_{sca}}{4\pi d^2} \begin{pmatrix} P_{11} & P_{12} & P_{13} & P_{14} \\ P_{21} & P_{22} & P_{23} & P_{24} \\ P_{31} & P_{32} & P_{33} & P_{34} \\ P_{41} & P_{42} & P_{43} & P_{44} \end{pmatrix} \begin{pmatrix} I_i \\ Q_i \\ U_i \\ V_i \end{pmatrix}$$

$C_{sca}$  = scattering cross section

$d$  = distance from the scatterer

$P$  = phase matrix

# Polarimetric & photometric observations



Rougier (1933), Lyot (1929)