1st exercises for DAIM'2014

Ex. 1

Show with Venn diagram for events A and B that

a) $A = AB^C + AB$

b) $A \cup B = AB^C \cup A^C B \cup AB$

c) Use axiom 1.3 from material to items a) (for *A* and *B*) and b), and derive the addition rule for two events in Eq. 1.4: $P(A \cup B) = P(A) + P(B) - P(AB)$.

Ex. 2

Let's assume that $P(A|B) = P(A|B^C)$. Show that then $A \perp B$.

Ex. 3

Show that $P(A) \leq 1 - P(A^C \cap B^C) \leq P(A) + P(B)$. Hints: Total probability says that $P(S) = 1, A \cup A^C = S$. You can use Venn diagrams for certain steps.

Ex. 4

There is 5 white and 10 black balls in a bowl. Ball is lifted, color checked, and returned to bowl. This is done 10 times. What is the probability to receive a) at least one white ball, b) five white balls?

Ex. 5

Prove that E(aU + b) = aE(U) + b for random variable U and constants a, b. Use Eq. 1.17.

Ex. 6

Compute E(*Y*), when distribution for *Y* is a) $f(y) = \frac{1}{2} \exp(-|y|), y \in \mathbb{R}$ b) $f(y) = 8/y^3, y > 2$ c) $f(y) = y \exp(-\frac{1}{2}y^2), y > 0$

Ex. 7

Let *U* have uniform distribution between (-1, 1), so $f_U(u) = 1/2$. What is the distribution of transformed variable $V = U^2$?

Ex. 8

Download the datafile two-variable.dat and make report (including, e.g., statistics of the two variables (columns), dependence, plots...)