



Crash course in X-ray imaging

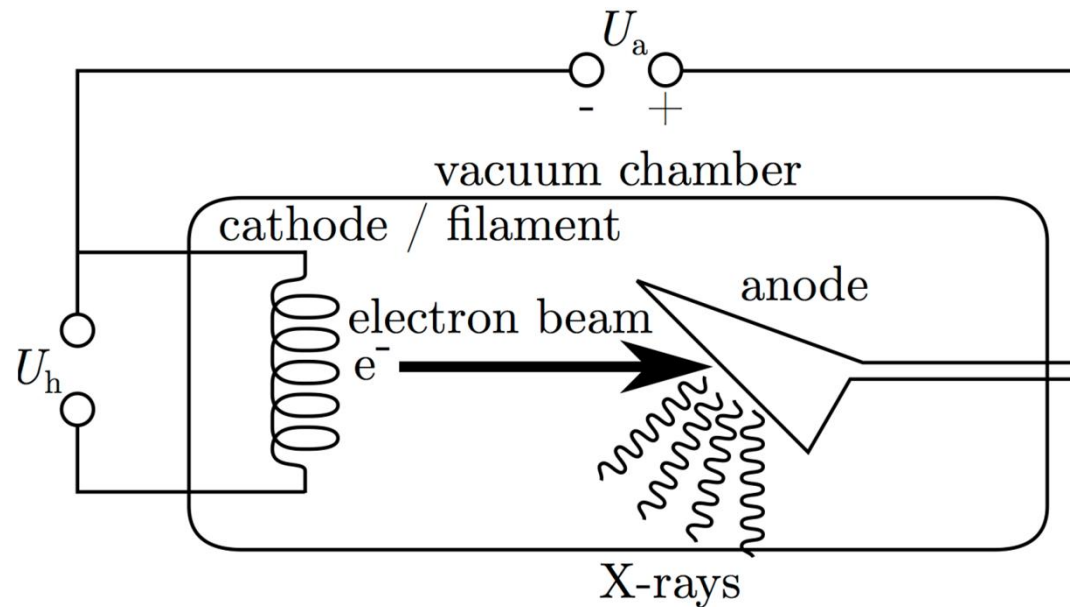
Alexander Meaney

Inverse Problems course 2015

6.2.2015



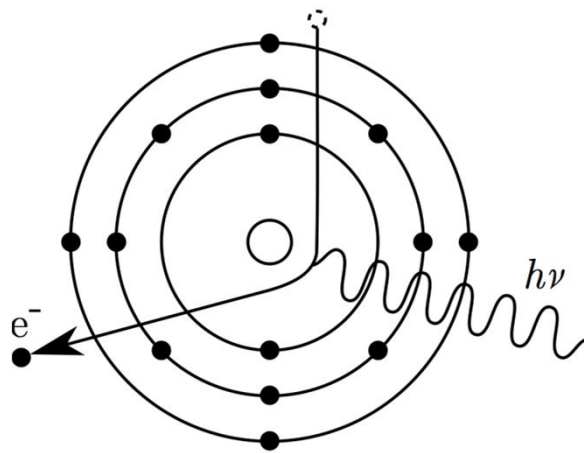
X-ray generation, part I: The X-ray tube



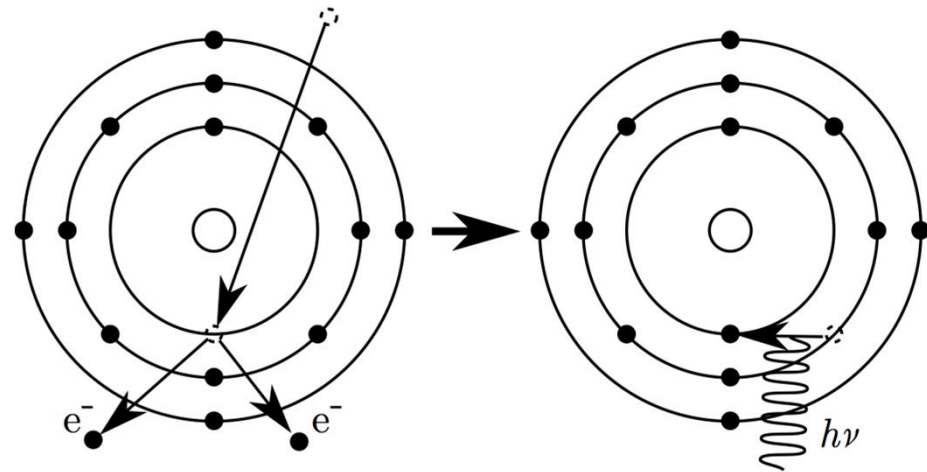


X-ray generation, part II

Electron-matter interactions



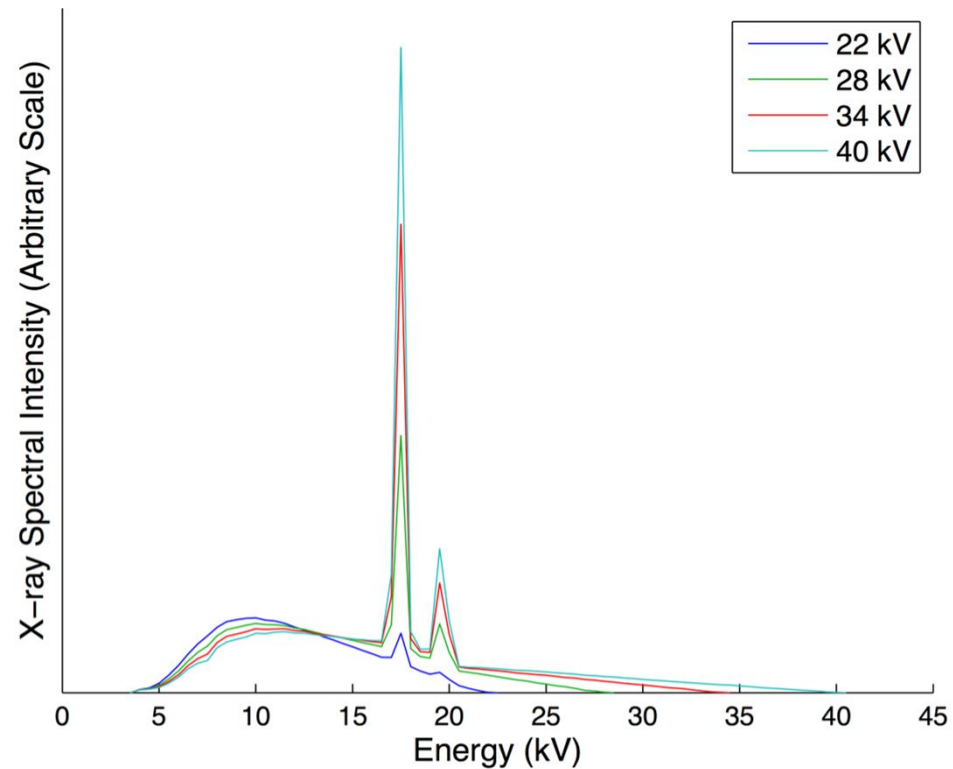
Bremsstrahlung



Characteristic X-rays

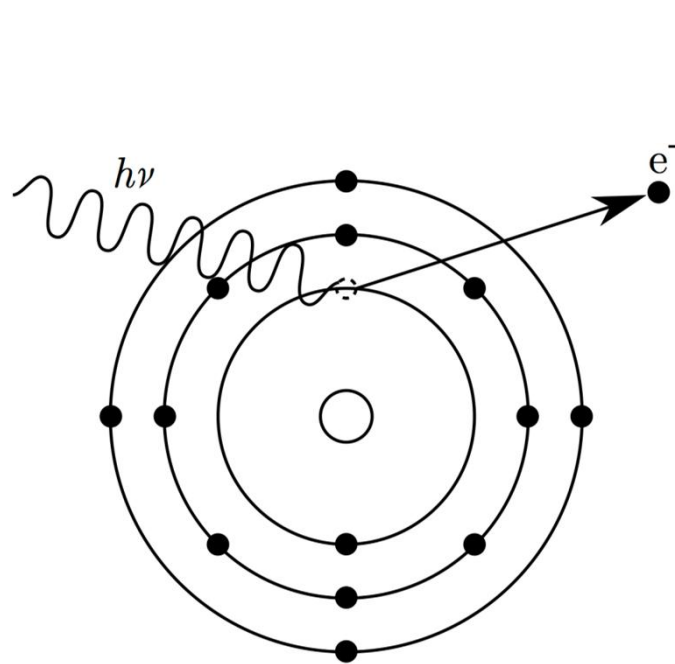


X-ray generation, part III: Mo target energy spectrum

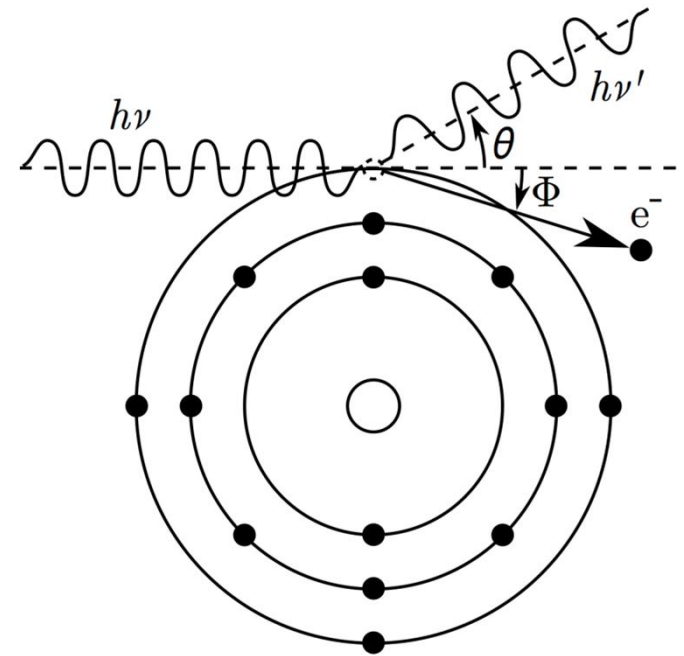




Photon-matter interactions



Photoelectric effect



Compton scattering



X-ray attenuation, part I: Beer-Lambert Law

- X-ray attenuation in matter is described by the *Beer-Lambert law*
- In homogenous matter:

$$I = I_0 e^{-\mu s}$$

- In heterogenous matter:

$$I = I_0 e^{-\int_{ray} \mu(x,y) ds}$$
$$\rightarrow -\ln\left(\frac{I}{I_0}\right) = \int_{ray} \mu(x,y) ds$$

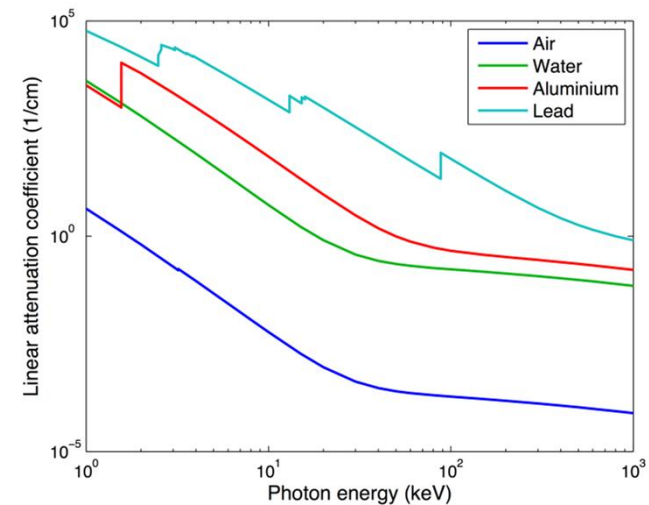


X-ray attenuation, part II: Energy dependency

- Attenuation coefficients are a function of energy E
→ The Beer-Lambert law must be corrected:

$$I = I_0(E) e^{-\int_{ray} \mu(x, y, E) ds} dE$$

- It is usually assumed in tomography that μ is energy independent
→ This can lead to imaging artefacts



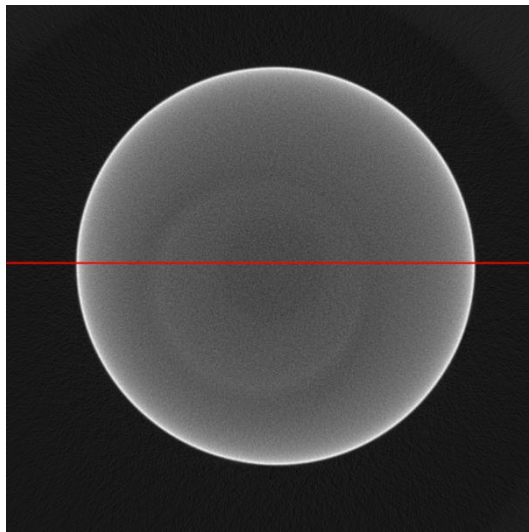


X-ray attenuation, part III: X-ray projection image

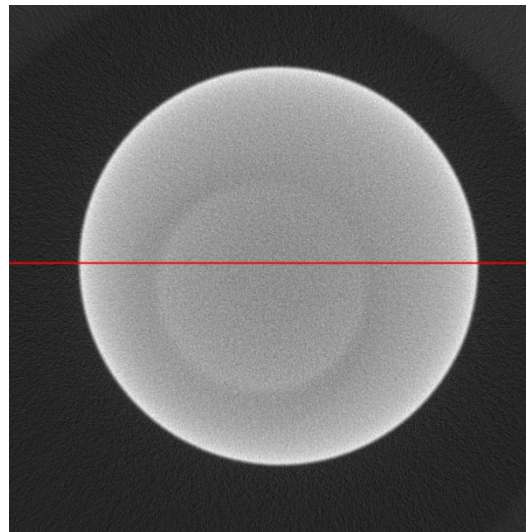




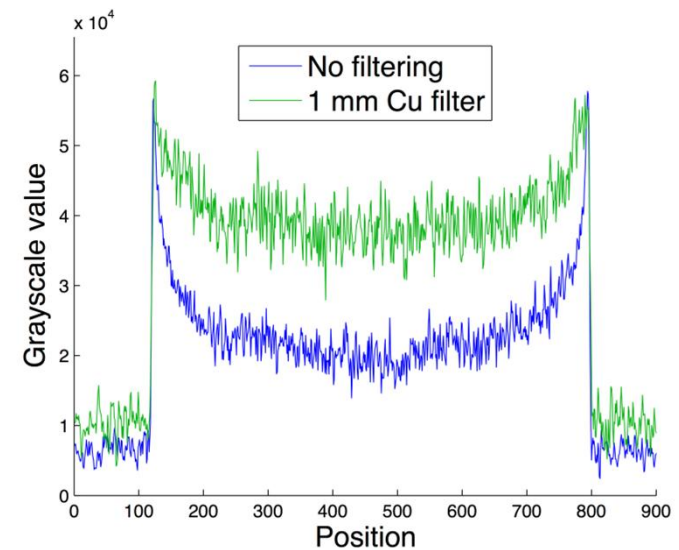
X-ray attenuation, part IV: Beam-hardening artefacts



No filter

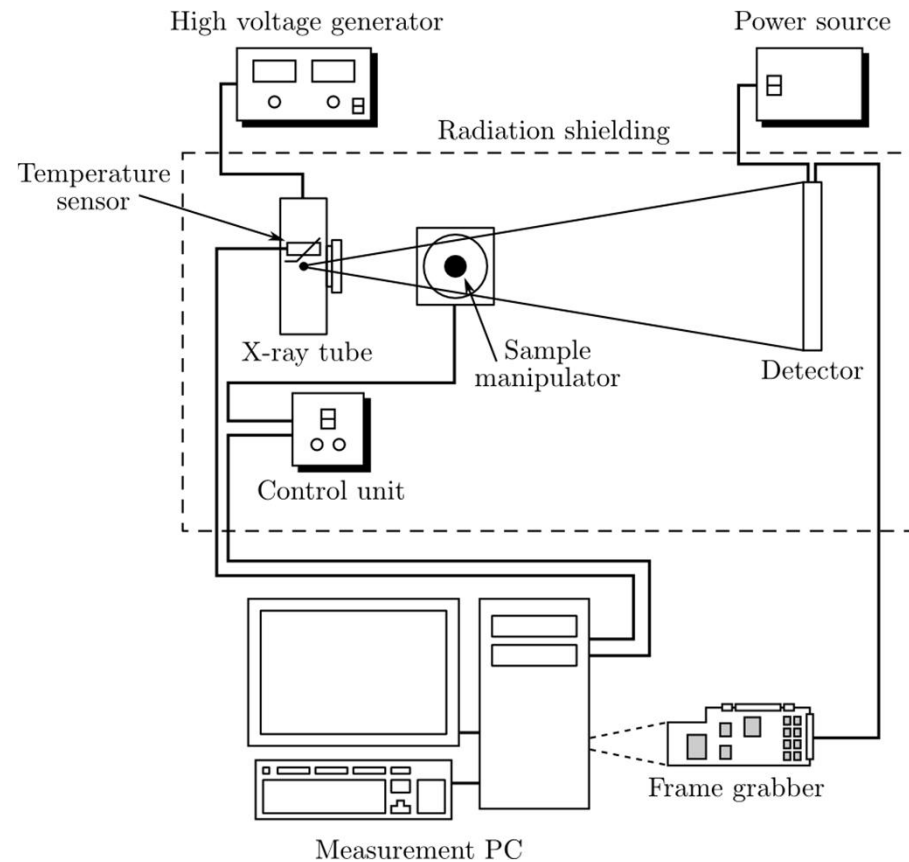


1 mm Cu filter





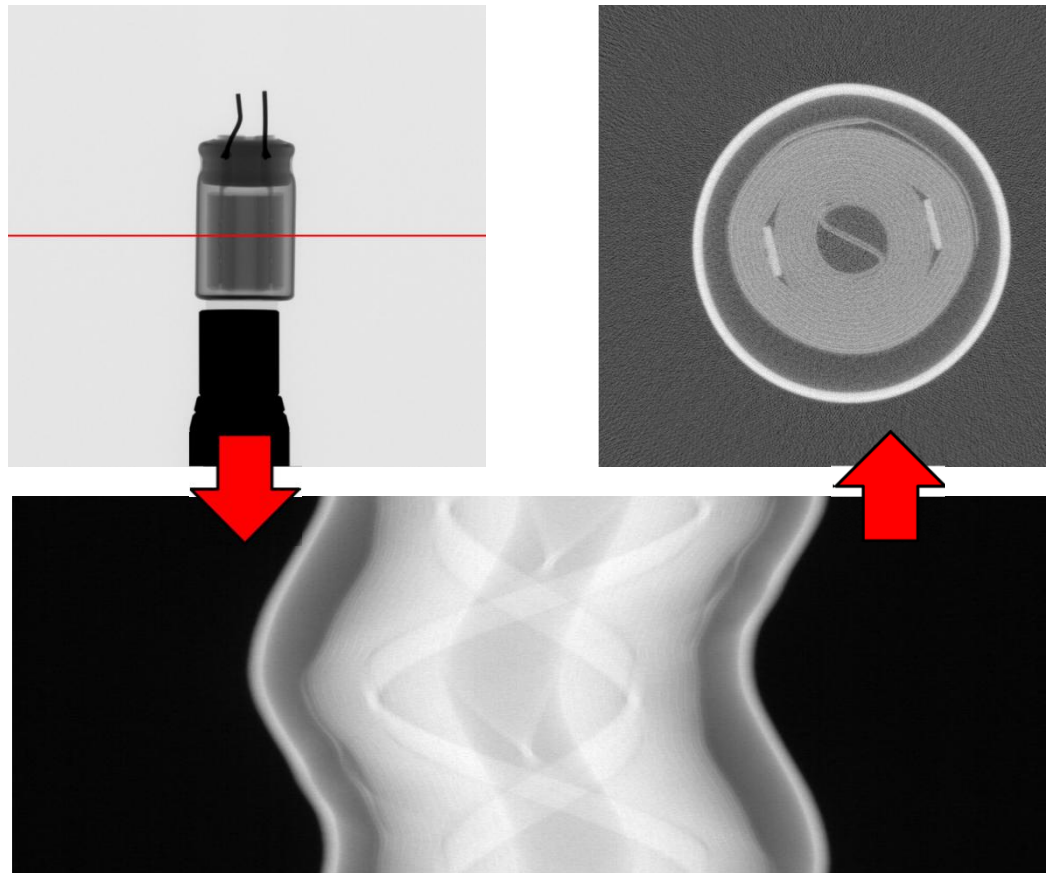
Industrial Mathematics Computed Tomography (CT) Laboratory





CT Reconstruction: Projections \rightarrow sinogram \rightarrow slice

Effective pixel size
 $= 26.1 \mu\text{m}$





Questions?

eg

