



Galaxy formation and evolution

PAP 318, 5 op, autumn 2020
on Zoom

**Lecture 9: Star formation and supernova
feedback in galaxies – Additional notes,
06/11/2020**



Lecture 9 additional notes I

- Page 4: In the Milky Way the observed star formation rate, $\text{SFR} \sim 1 M_{\odot} / \text{yr}$, but if gas would be collapsing on the free-fall time the SFR would be $\text{SFR} \sim 100 M_{\odot} / \text{yr}$, i.e. 100x higher.

- Page 5: Virial theorem without external pressure

$$2K + W = 0, \quad K = \frac{3}{2} N k_b T = \frac{3}{2} M c_S^2, \quad W = -\frac{3}{5} \frac{GM^2}{r_{cl}}$$

- Page 5: Derivation of the Jeans mass:

$$\bar{\rho} = \frac{3M}{4\pi r^3}, \quad M_J = \frac{4\pi}{3} \left(\frac{\lambda_J}{2} \right)^3 \rho, \quad \lambda_J = c_S \left(\frac{\pi}{G\rho} \right)^{1/2}$$



Lecture 9 additional notes II

- Page 5: Derivation of the Jeans mass continued

$$M_J = \frac{\pi}{6} c_S^3 \left(\frac{\pi}{G} \right)^{3/2} \rho^{-1/2}$$

- Page 8: The turbulence in GMCs is supersonic due to the very low gas temperatures, corresponding to low thermal velocities (~0.2 km/s). Thus the supporting velocity is due to turbulence not thermal motions.
- The Mach parameter M can enhance overdensities ρ' over the mean density:

$$\mathcal{M} = v_{\text{gas}}/c_S, \quad \rho' = \mathcal{M}^2 \bar{\rho}$$



Lecture 9 additional notes III

- Page 12: **Adsorption** is the adhesion of atoms, ions or molecules from a gas, liquid or dissolved solid to a surface (in this case the surface of dust grains).
- Page 18: Schmidt-Kennicutt law, star formation controlled by the self-gravity of the gas.

$$\text{SFR} = \epsilon_{\text{SF}} \times \rho_{\text{gas}} / t_{\text{ff}}, \quad t_{\text{ff}} \propto \rho^{-1/2}, \quad \text{SFR} \propto \rho^{1.5}$$

- Page 22: Supernova feedback: (c =NFW halo concentration)

$$E_{\text{fb}} = \epsilon_{\text{SN}} \zeta M_* E_{\text{SN}}, \quad E_{\text{ej}} = \frac{1}{2} M_{\text{ej}} v_{\text{esc}}^2, \quad V_{\text{esc}} \simeq \sqrt{6c} V_{\text{vir}}$$



Lecture 9 additional notes IV

- Page 22: Supernova feedback continued

$$\epsilon_{\text{SN}} \zeta M_* E_{\text{SN}} = \frac{1}{2} M_{\text{ej}} v_{\text{esc}}^2, \Rightarrow \frac{M_{\text{ej}}}{M_*} \simeq 0.4 \epsilon_{\text{SN}} \left(\frac{c}{10} \right)^{-1} \left(\frac{v_{\text{vir}}}{200 \text{ km/s}} \right)^{-2}$$

- Page 23: Supernova heating:

$$E_{\text{int}} = \frac{3}{2} M_{\text{gas}} \frac{k_B T}{\mu m_p}, \quad T_{\text{vir}} = \frac{\mu m_p}{2k_B} V_{\text{vir}}^2$$

$$E_{\text{reheat}} = \frac{3}{2} M_{\text{gas}} \frac{k_B (T_{\text{vir}} - T_{\text{init}})}{\mu m_p} = \frac{3}{4} M_{\text{gas}} V_{\text{vir}}^2 \left(1 - \frac{T_{\text{init}}}{T_{\text{vir}}} \right)$$



Lecture 9 additional notes V

- Page 23: Supernova heating continued

$$(V_{\text{esc}}/V_{\text{vir}})^2 \simeq 6c, \quad E_{\text{ej}} = \frac{1}{2}M_{\text{ej}}V_{\text{esc}}^2 = \frac{1}{2}M_{\text{ej}}6cV_{\text{vir}}^2$$

- Page 23: Equating the reheating energy to the ejection energy:

$$\frac{M_{\text{gas}}}{M_*} \simeq 17\epsilon_{\text{SN}} \left(\frac{v_{\text{vir}}}{200 \text{ km/s}} \right)^{-2} \left(1 - \frac{T_{\text{init}}}{T_{\text{vir}}} \right)^{-1}$$