



Galaxy formation and evolution

PAP 318, 5 op, autumn 2020
on Zoom

**Lecture 8: Formation and evolution of
gaseous haloes– Additional notes, 30/10/2020**



Lecture 8 additional notes I

- Page 4: Shock-heating: Initial Assumption

$$v_{\text{in}}^2 \gg \frac{k_B T_{\text{in}}}{\mu m_p}$$

- Page 4: μ is the mean molecular weight and m_p the proton mass.

$$N = \frac{M_{\text{gas}}}{\mu m_p}$$

- Page 5: Gas on free-fall:

$$\frac{1}{2} m v^2 - \Phi m = 0 \Rightarrow v_{\text{in}} \simeq v_{\text{esc}}(r_{\text{sh}}) = \sqrt{2|\Phi(r_{\text{sh}})|}$$



Lecture 8 additional notes II

- Page 5: Definition of the virial velocity:

$$v_{\text{vir}}^2 = \frac{GM_{\text{vir}}}{r_{\text{vir}}}$$

- Page 6: Hydrostatic equilibrium:

$$\frac{k_b}{\mu m_p} \frac{d}{dr} (\rho T) = -\rho \frac{GM(r)}{r^2}$$

$$M(r) = -\frac{k_b r^2}{\mu m_p G \rho} \left(\frac{d\rho}{dr} \cdot T + \frac{dT}{dr} \cdot \rho \right)$$



Lecture 8 additional notes III

- Page 7: Correcting for non-thermal pressure, add the term:

$$\frac{P_{\text{nt}}}{P_{\text{th}}} \frac{d \ln P_{\text{nt}}}{d \ln r}$$

- Page 8: The terms going into the virial temperature formula:

$$2K = 3 \frac{M_{\text{gas}}}{\mu m_p} k_B T_{\text{vir}} \quad W = \zeta \frac{GM_{\text{gas}} M_{\text{vir}}}{r_{\text{vir}}}$$

$$\Sigma = V \cdot P = \frac{4\pi}{3} r_{\text{cl}}^3 \cdot 3P_{\text{ext}} = 4\pi r_{\text{cl}}^3 P_{\text{ext}}$$